

# 1C3 Design of bridges

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# List of lectures

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1. History and types of steel bridges
2. Fundamental terms
3. Basis of design
4. Bearings, expansion joint, bridge accessories
5. Bridge deck
6. Plate girder steel bridges 1
7. Plate girder steel bridges 2
8. Plate girder steel bridges 3
9. Composite steel-concrete bridges 1
10. Composite steel-concrete bridges 2
11. Truss girder bridges
12. Pedestrian footbridges
13. Examples of bridge structures

# Objectives of the lecture 9

- basic principles
- global analysis
- ultimate limit states
- serviceability limit states
- examples



Objectives  
Basic principles

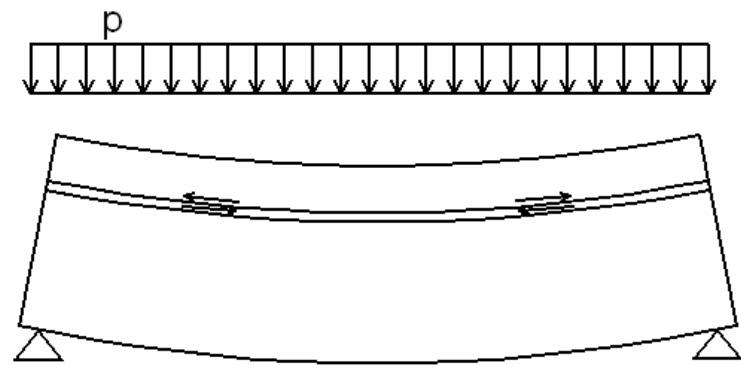
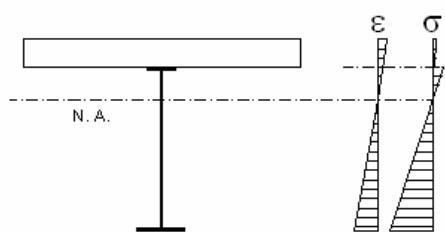
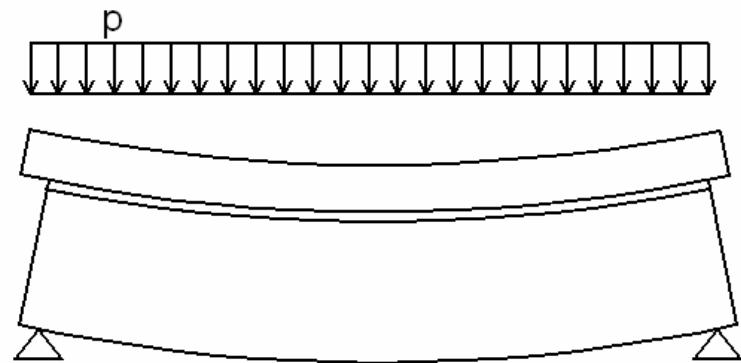
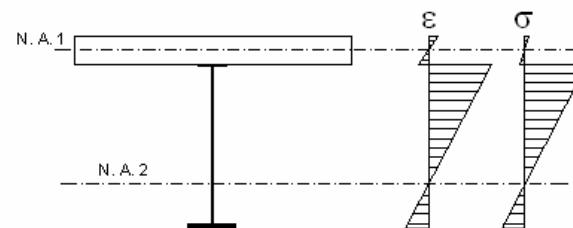
Global analysis

ULS

SLS

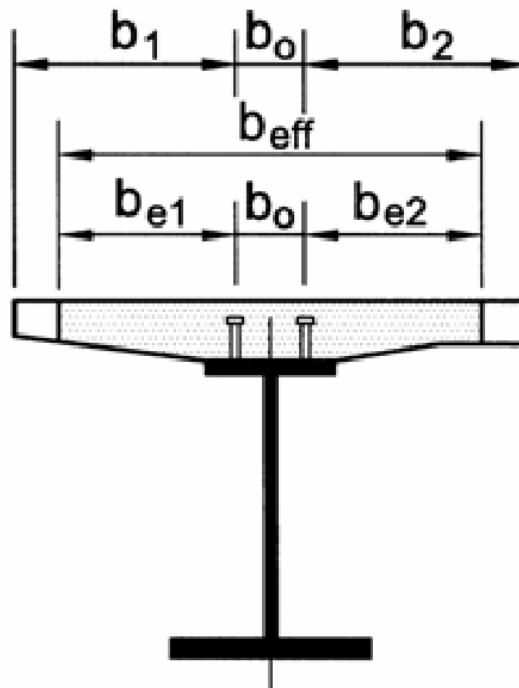
Examples

# Basic principles



# Global analysis

Effective width of concrete deck

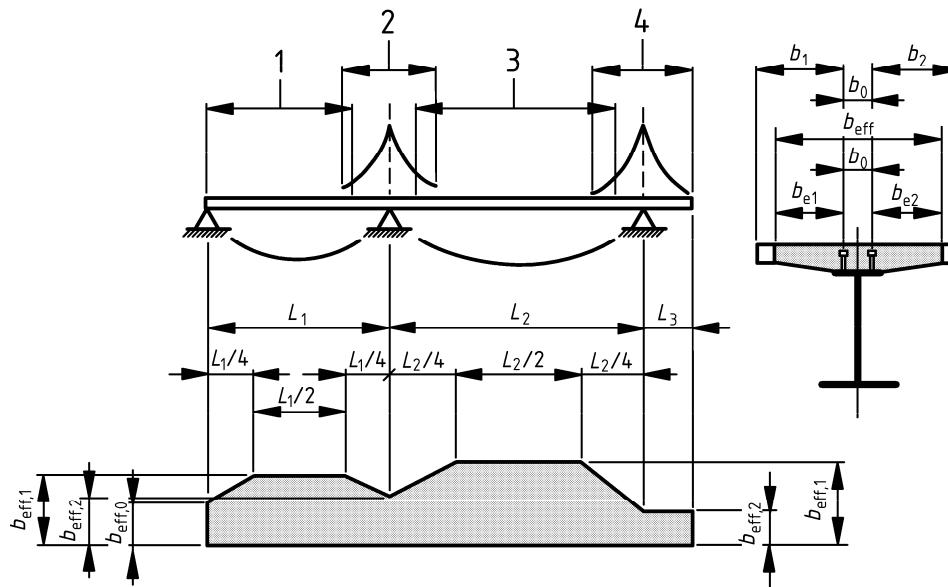


$$B_{eff} = \min[(b_1 + b_o + b_2); (b_{e1} + b_o + b_{e2})]$$

$$b_{e1} = L/8$$

# Global analysis

Multispan bridge – effective width



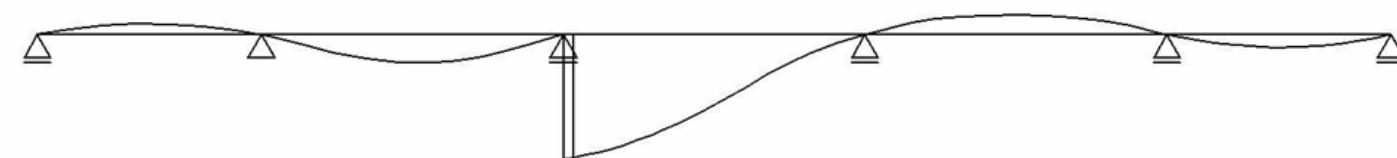
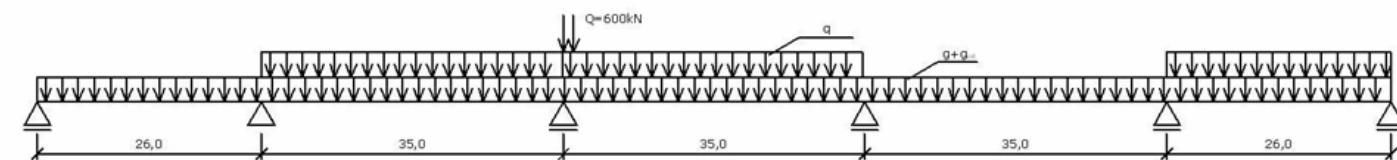
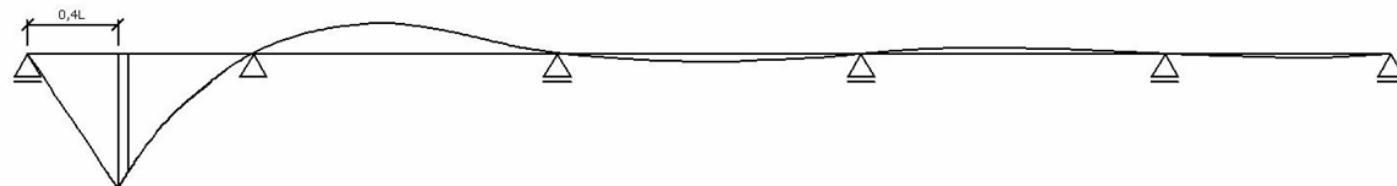
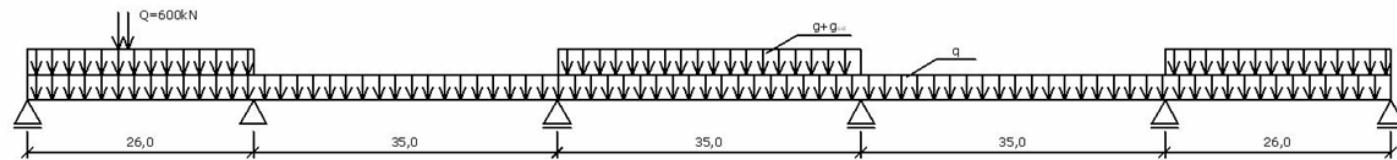
- 1  $L_e = 0,85 L_1$  for  $b_{eff,1}$
- 2  $L_e = 0,25 (L_1 + L_2)$  for  $b_{eff,2}$
- 3  $L_e = 0,70 L_2$  for  $b_{eff,1}$
- 4  $L_e = 2L_3$  for  $b_{eff,2}$

$$b_{eff} = b_0 + \sum \beta_i b_{ei}$$

$$\beta_i = (0,55 + 0,025 L_e / b_{ei}) \leq 1,0$$

# Global analysis

## Multispan bridge – influence lines (example)



Objectives  
Basic principles

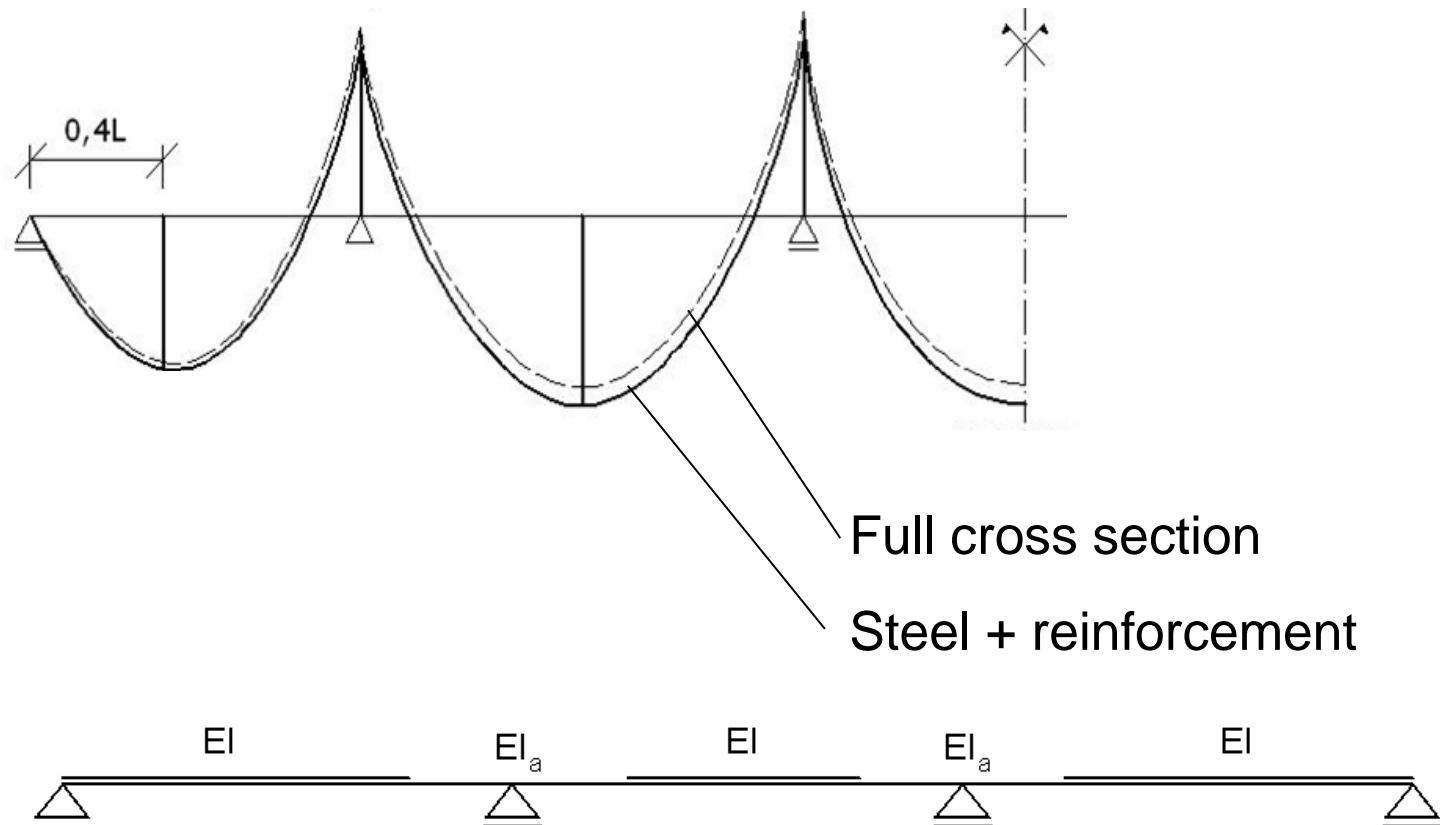
## Global analysis

ULS

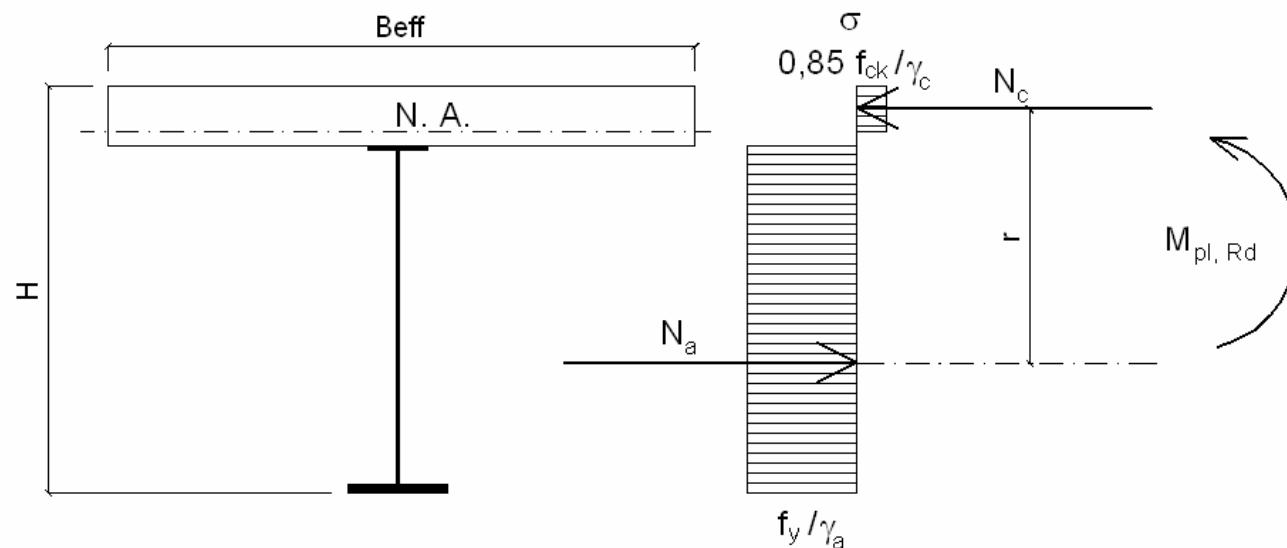
SLS

Examples

### Redistribution of moments



## 1. Neutral axis in concrete, positive moment



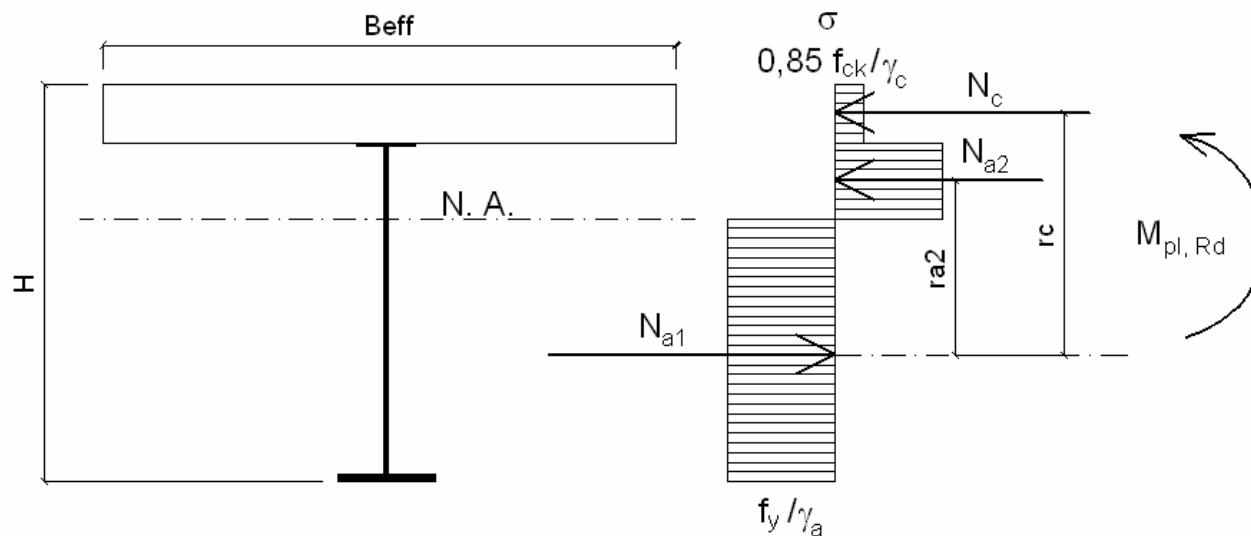
$$N_{c,f} = N_{pl,a}$$

$$0,85 \cdot B_{eff} \cdot x \cdot f_{c,k} / \gamma_c = A_a \cdot f_y / \gamma_a$$

$$M_{pl,Rd} = N_a \cdot r = N_c \cdot r$$

# ULS

## 2. Neutral axis in steel, positive moment



$$N_c + N_{a2} = N_{a1}$$

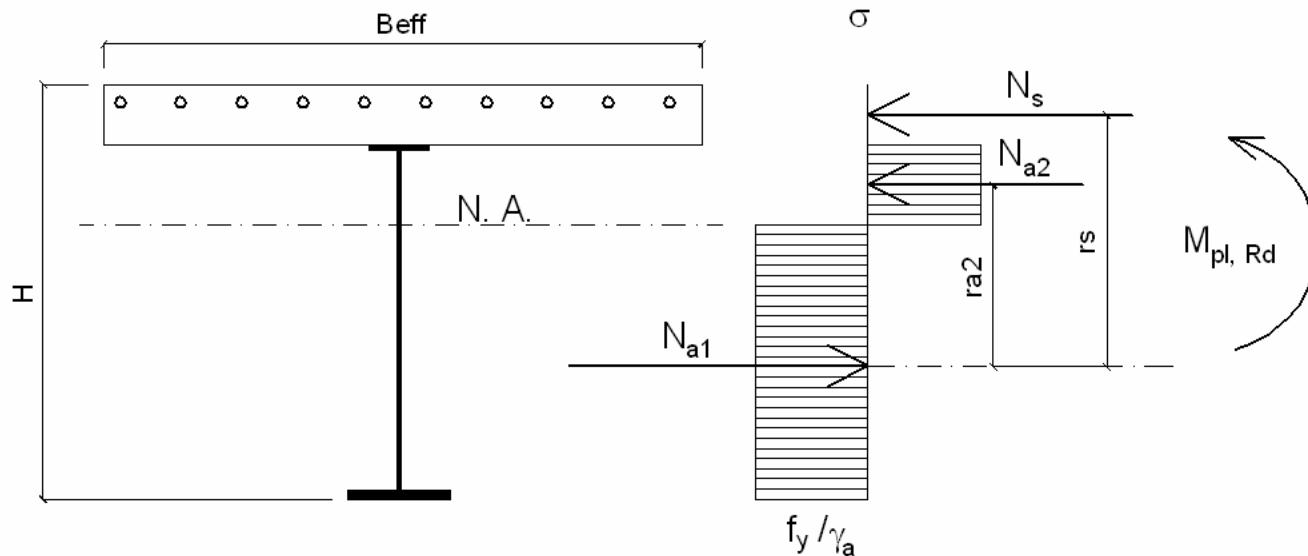
$$0,85 \cdot A_c \cdot f_{c,k} / \gamma_c + A_{a2} \cdot f_y / \gamma_a = A_{a1} \cdot f_y / \gamma_a$$

$$M_{pl,Rd} = N_c \cdot r_c + N_{a2} \cdot r_{a2}$$

# ULS

ULS  
SLS  
Examples

## 3. Neutral axis in steel, negative moment



$$N_s + N_{a2} = N_{a1}$$

$$A_s \cdot f_s / \gamma_s + A_{a2} \cdot f_y / \gamma_a = A_{a1} \cdot f_y / \gamma_a$$

$$M_{pl,Rd} = N_s \cdot r_s + N_{a2} \cdot r_{a2}$$

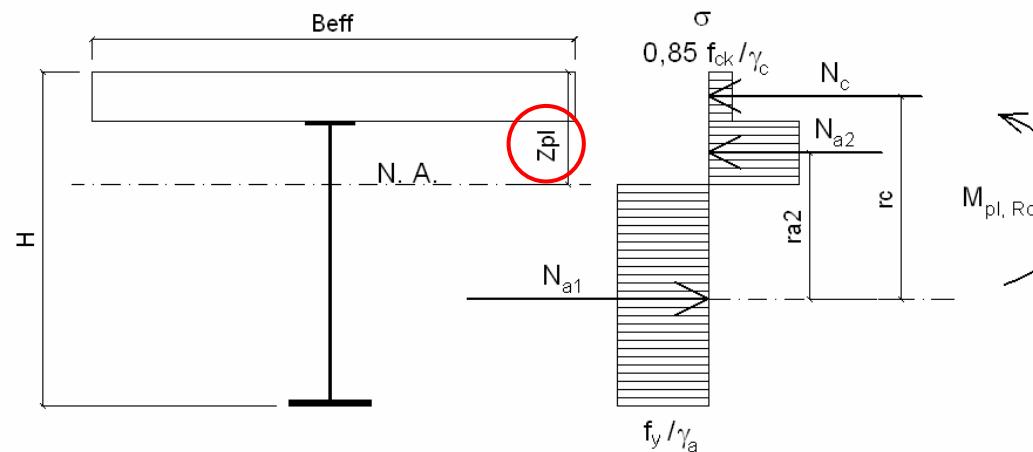
# **ULS**

ULS

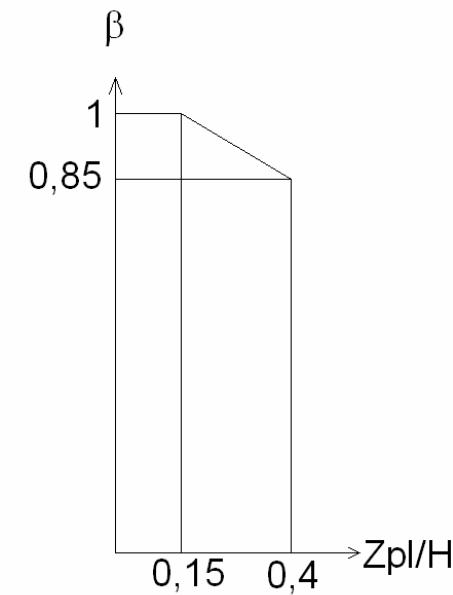
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## Examples

## Reduction of moment resistance



$$M_{pl,Rd} = \beta (N_c \cdot r_c + N_{a2} \cdot r_{a2})$$



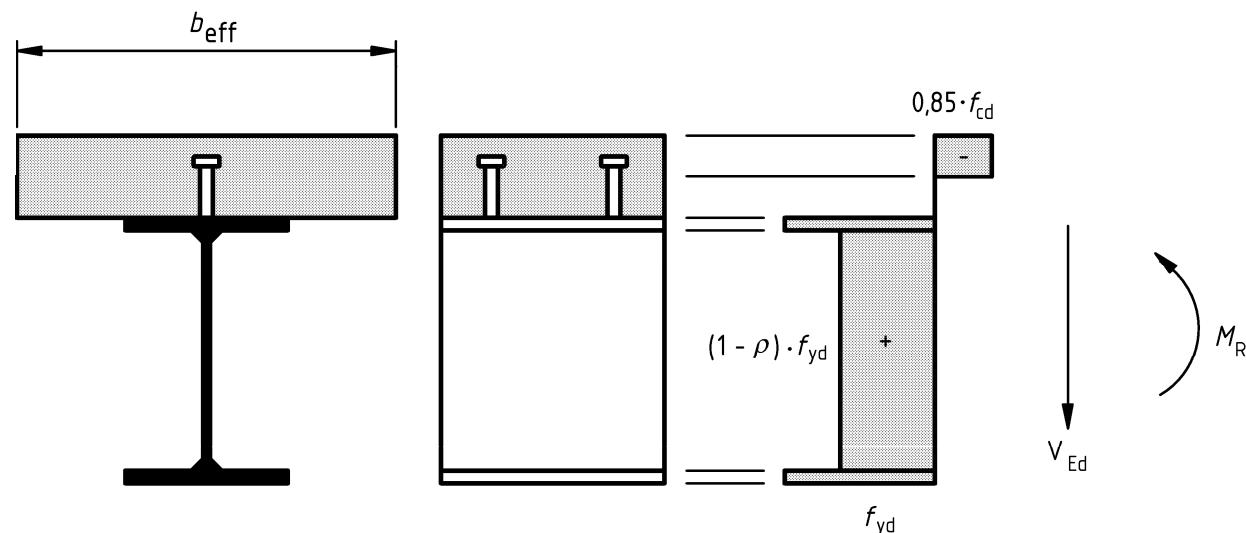
# ULS

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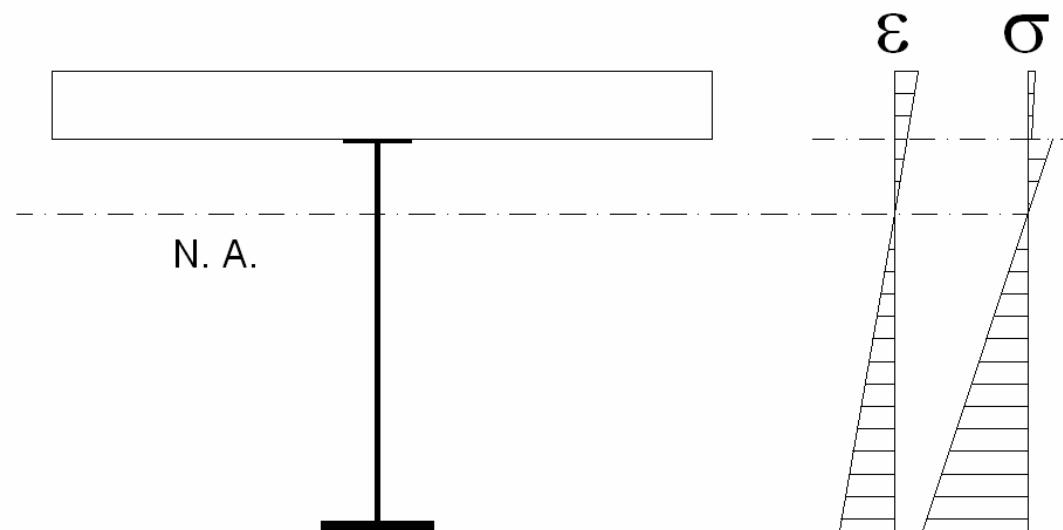
Examples

$$\rho = (2V_{Ed}/V_{Rd} - 1)^2$$



# Serviceability limit states

Deflection  
Stress  
(Web breathing)  
Visual impression



# Serviceability limit states

Elastic analysis:

- concrete relaxation
- short / long term loads
- effect of shrinkage

$$n_L = n_0 (1 + \psi_L \varphi_t)$$

$$n_0 = E_a / E_{cm}$$

# Serviceability limit states

Brandýsek: 3 spans, 2 x 5 beams



# Serviceability limit states

Mosty u Jablunkova



# Serviceability limit states

Ostrov



# Serviceability limit states

Děčín



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**Thank you  
for your kind attention**

# Notes to users of the lecture

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- This session is a basic information about actions on bridges and requires about 60 min lecturing.
- The use of relevant standards of national standard institutions are strongly recommended.
- Keywords for the lecture:  
composite bridge, shear connection, steel, concrete, road bridge, footbridge, railway bridge, Eurocodes.