



**CTU**

CZECH TECHNICAL  
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IN PRAGUE

# **Connection design by Component Based Finite Element Method**

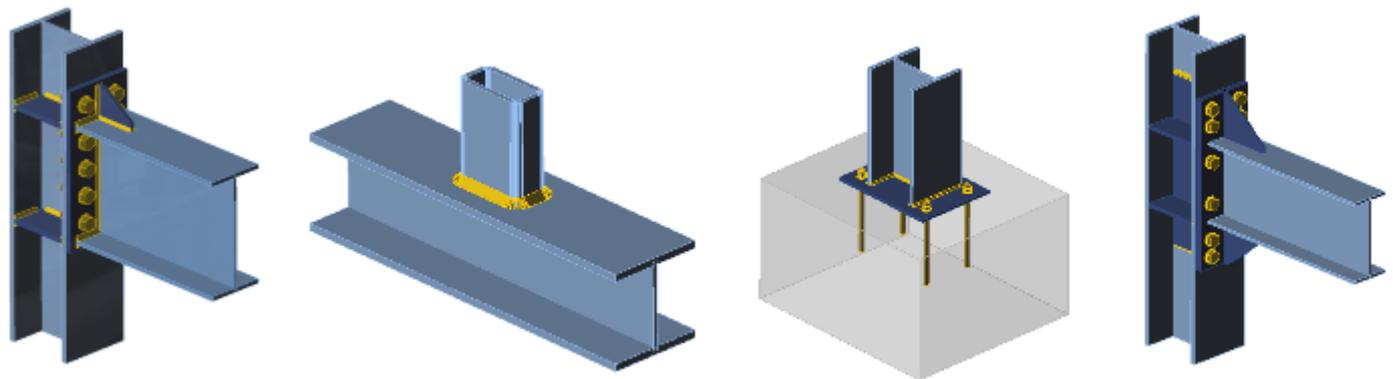
**Lecture 1**

**Beam to Column Moment Connection**

# List of lectures

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- 1) **Beam to column moment connection**
- 2) Joint of hollow to open section
- 3) Column base
- 4) Seismically qualified joints



# Aims and objectives

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- Provide information on joint modelling
- Introduce principles of CBFEM
- Provide an online training to students and engineers
- Illustrate differences between research and design oriented FEM
- Show the process of Validation & Verification
- Offer list of references relevant to the topic

# **Beam to column moment connection**

**František Wald, Lukáš Gödrich, Marta Kuříková,  
Lubomír Šabatka, Jaromír Kabeláč, Drahoš Kojala**

# Tutorial

- This lecture describes principles of **FEA modelling** of beam to column moment connection.
- Survey of both simple and FEM analyses and modelling are shown.
- Finally Validation, Verification and Benchmark case is presented.

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# Outline of the lecture

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- **Introduction to design**
  - Design models
  - Global analyses
  - Classification
  - Component method
  - Interaction of internal forces
  - Assessment I
- **Component Based Finite Element Method**
  - General
  - Validation
  - Verification
  - Benchmark case
  - Assessment II
- **Summary**

# **Introduction to design**

## **Lecture 1**

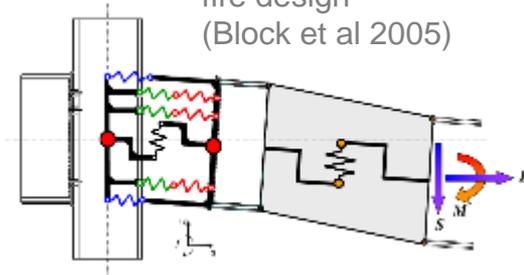
### **Beam to column moment connection**

# Past and Present design models

For joint design are available models:

- Experimental - history and contemporary design
- Curve fitting – currently hollow section joints design
- Analytical models
  - **Component Method (CM)**
- Research oriented finite element method
- Design oriented finite element method
  - **Component based FE Method (CBFEM)**

An example of component model for fire design (Block et al 2005)



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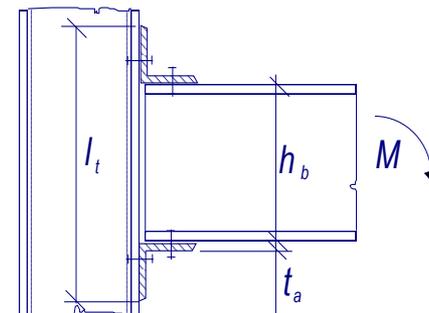
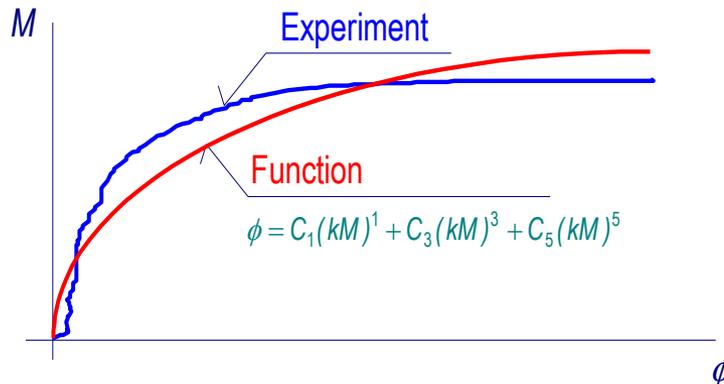
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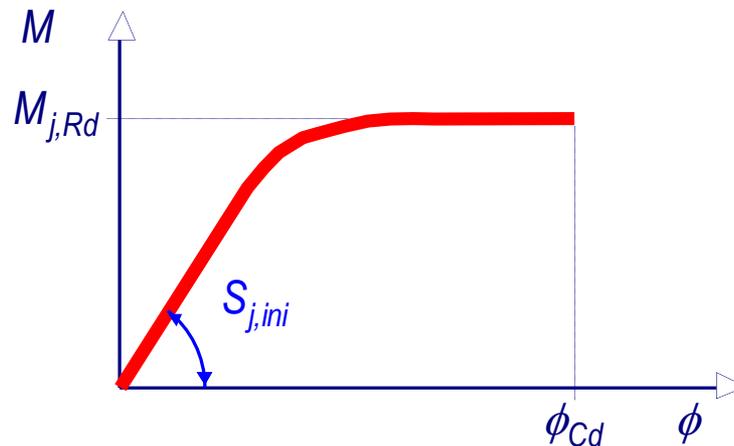
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An example of curve fitting model, Kishi and Chen (1990)

# Joints characteristics in bending

- Major characteristics for joint in bending are
  - **Initial stiffness**  $S_{j,ini}$ 
    - Small influence to distribution of internal forces
  - **Design resistance**  $M_{j,Rd}$ 
    - Direct influence to resistance
  - **Deformation capacity**  $\phi_{Cd}$ 
    - Influence to plastic and seismic design only



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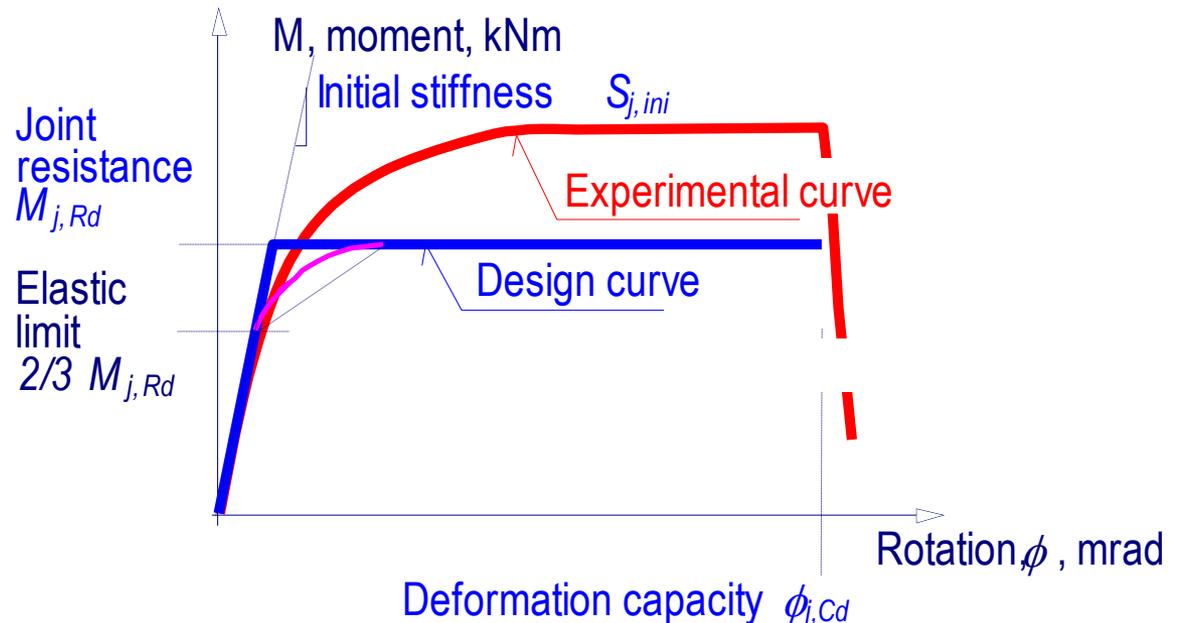
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# Design model and experimental behaviour

- The design model reflects the need of designers to safe prediction of joint behaviour
- As structural elements are in joint designed for its material yielding  $f_y$  or its ultimate stress  $f_u$
- The experimentally reached resistance is never the asked design resistance



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# Joints deformability/stiffness

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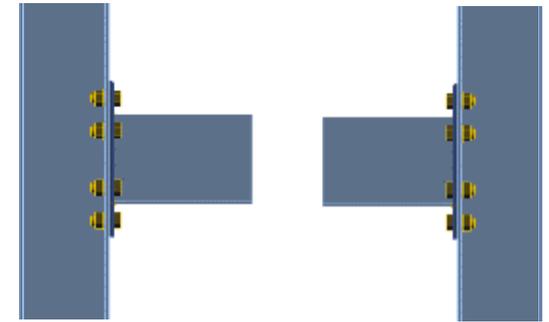
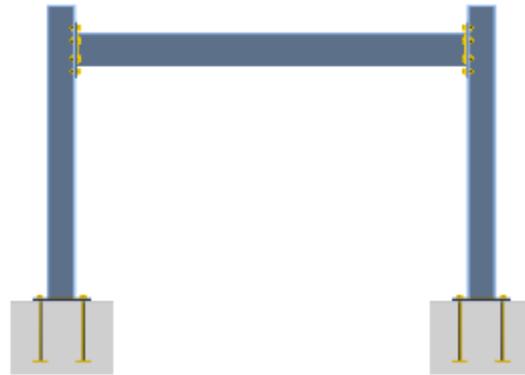
Assessment II

## Summary

- Joint deforms due to
  - **Shear force**
    - No influence to global distribution of internal forces
    - Is closed during erection
  - **Normal force**
    - No influence to global distribution of internal forces
    - Exception in space structures of course
  - **Bending moment**
    - Significant influence to distribution of internal forces
    - The highest is in rectangular closed frames

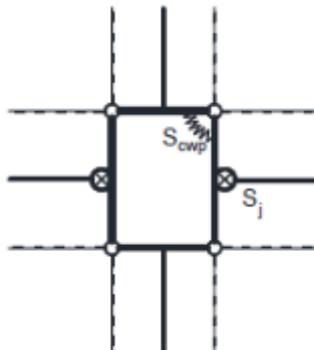
# Joints in global analyses

- Example of frame with its joints

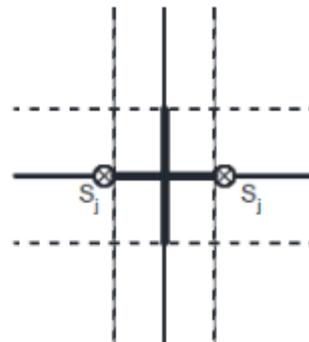


- If part of joint is flexible is in global analyses modelled as

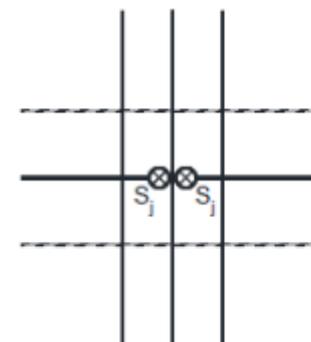
Flexible column web panel and semi-rigid connections



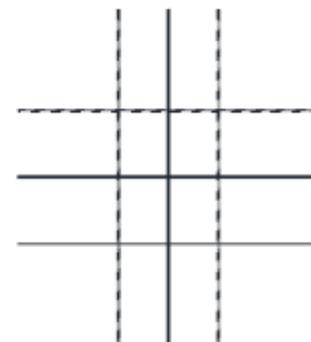
Stiff column web panel and semi-rigid or pinned connections



Stiff column web panel and semi-rigid or pinned connections



Stiff column web panel and rigid connections



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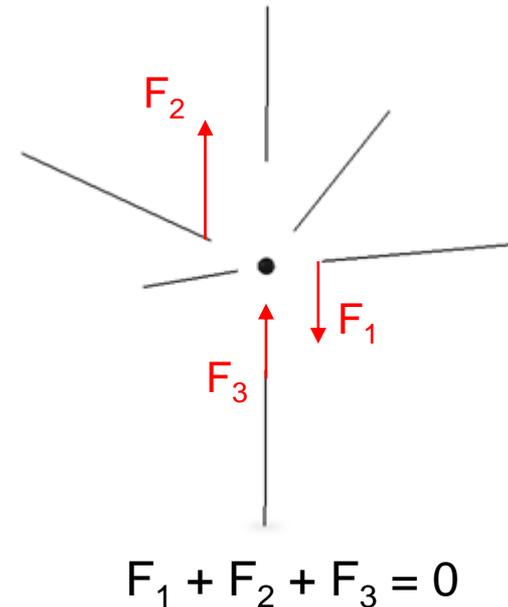
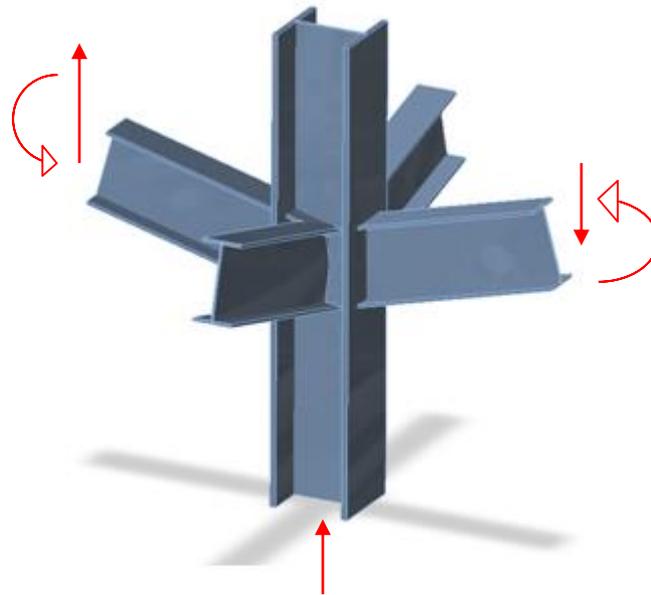
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# Physical and theoretical joint

- In global analyses with 1D members are forces transferred to beam ends.
- Forces are kept and moments are modified by action of forces on actual arms.
- Theoretical joint should be in equilibrium, see example right below.



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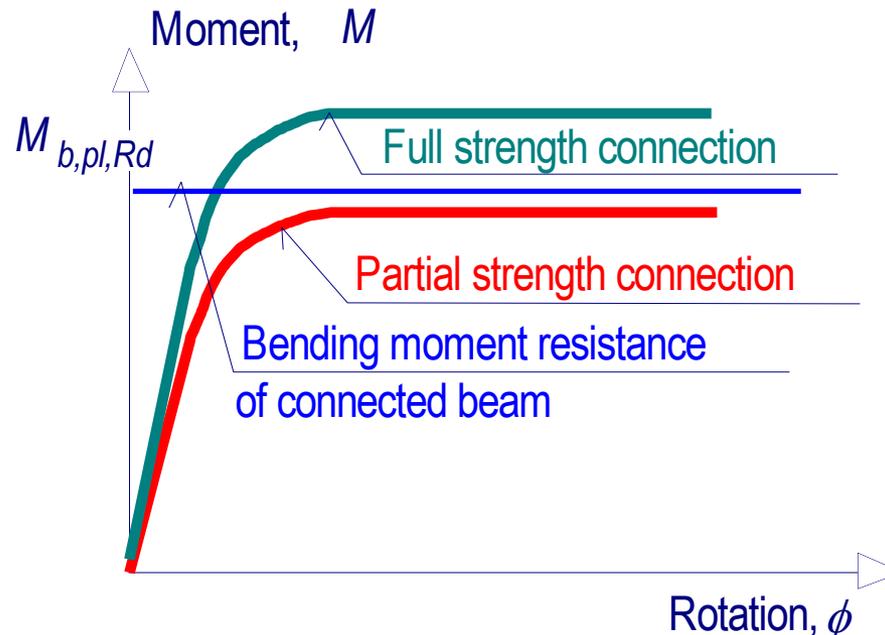
## Summary

- For global analyses of steel frames are joints classified to simplify the modelling.  
(Preferable as pinned and rigid joints.)
- According to Ch. 5 in EN1993-1-8:2006 are joints classified based on
  - Best engineering practice
  - Simplified assumption of frame behaviour
  - Actual influence of particular joint to frame design.  
(This implicates recalculation.)

# Classification based on resistance

- Bending moment resistance of connection to bending moment resistance of connected beam is compared in connections loaded in bending.

- Full strength joints/connections  $M_{j,Rd} > M_{b,pl,Rd}$
- Partial strength joints/connections  $M_{j,Rd} < M_{b,pl,Rd}$



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# Classification based on rotational capacity

- Rotational capacity of connection to rotational capacity of connected beam is compared in connections loaded in bending.

- Ductile connection
- Semi-ductile connection
- Brittle connection

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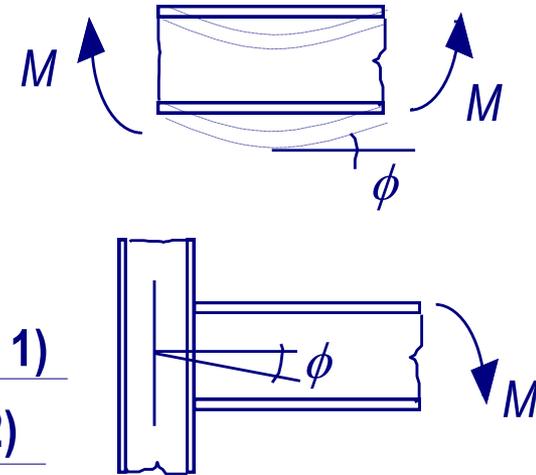
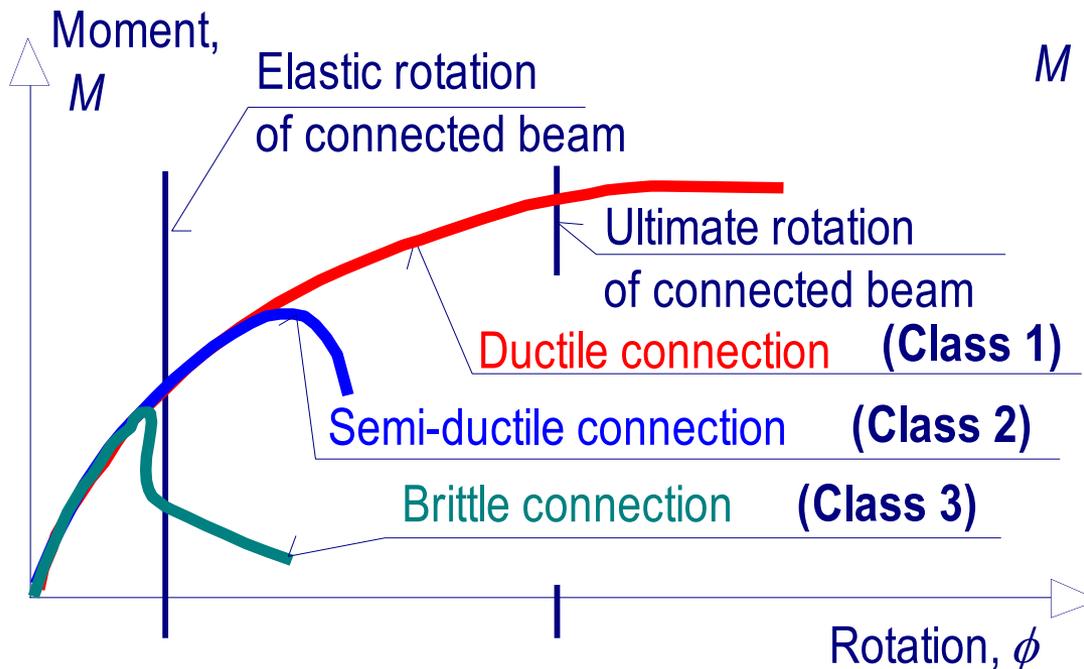
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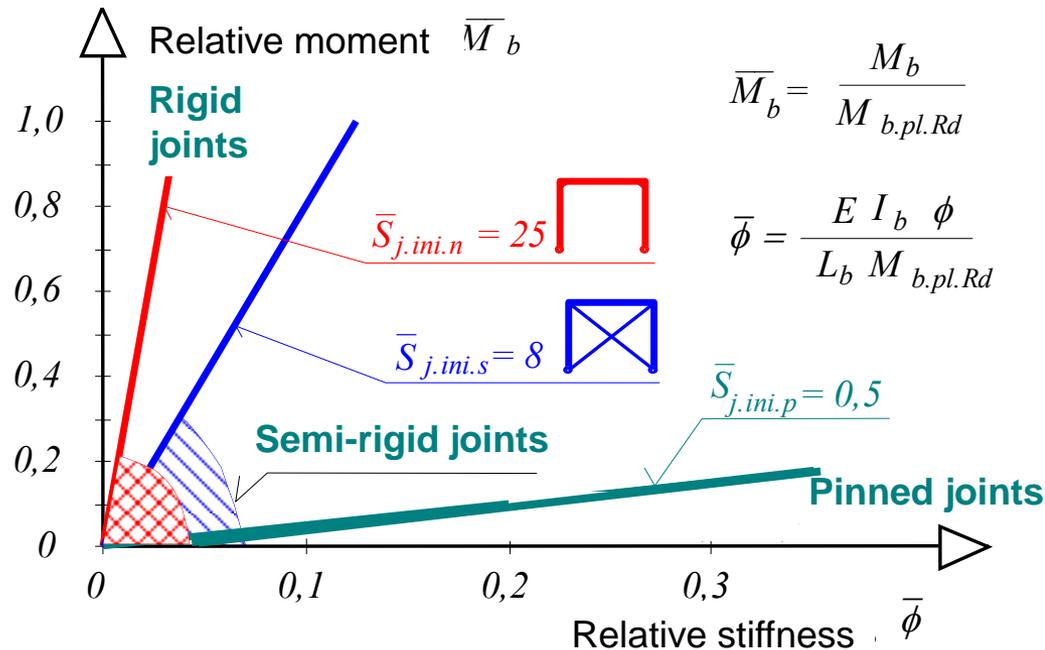
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# Classification based on stiffness

- Bending stiffness of connection to bending stiffness of connected beam is compared in connections loaded in bending.

- Rigid joint  $S_{j,ini} \geq 25 E I_b / L_b$  (for frames without bracing)
- Semi-rigid joint  $S_{j,ini,rigid} \leq S_{j,ini} \leq S_{j,ini,pinned}$
- Nominally pinned joint  $S_{j,ini} \leq 0,5 E I_b / L_b$



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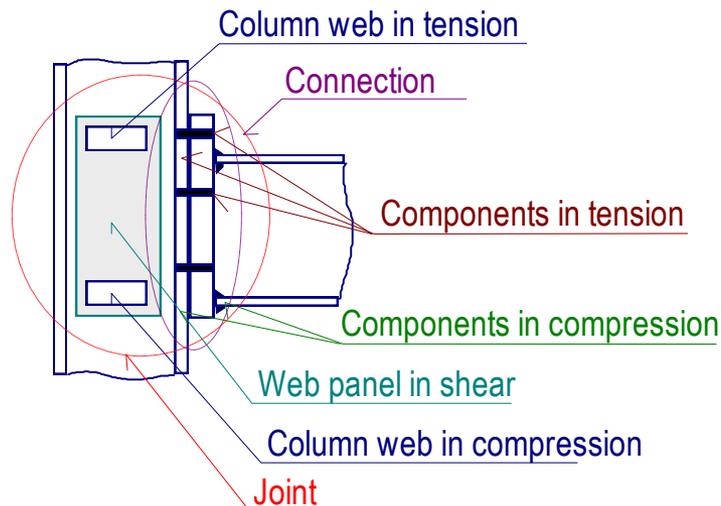
## Summary

# Component Method

- Component method is analytical procedure to evaluate joint resistance and stiffness.

It consist of steps:

- 1) **Decomposition of joint** to individual components based on assumed distribution of internal forces.
- 2) **Component description** in terms of deformational stiffness and resistance.
- 3) **Joint behaviour assembly** from the behaviour of its components based on assumed distribution of internal forces.



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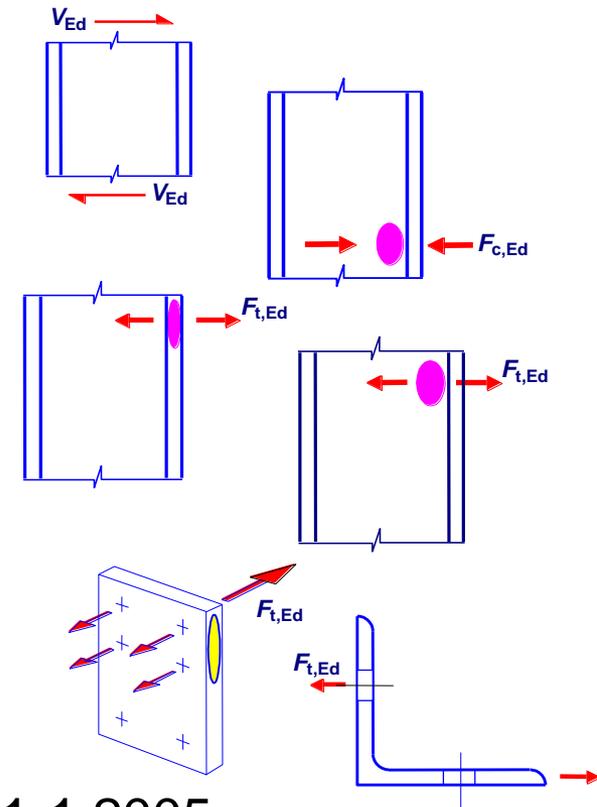
## Summary



## 2) Component description

- The structural properties of basic joint components are described in Chapter 6 of EN 1993-1-8 for some basic components, eg. for

- Column web panel in shear
- Column web in transverse compression
- Column web in transverse tension
- Column flange in bending
- End-plate in bending
- Flange cleat in bending



- For composite joints are in EN1994-1-1:2005
- For another joints in literature

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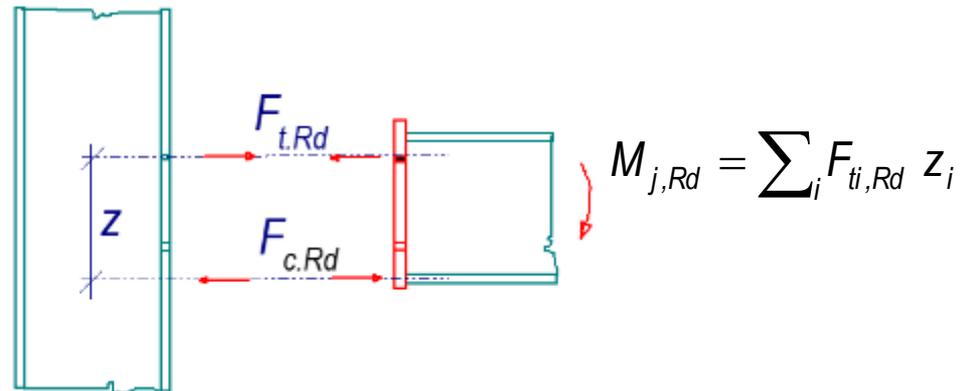
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### Summary

# 3) Joint assembly

- Joint are assembled using the assumed lever arms of components  $z_x$  assumed according to best engineering practice
- E.g. for bolted connection with one bolt row may be guess simplified assembly
  - $F_{c,Rd}$  is compression force recon in the middle of bottom flange
  - $F_{t,Rd}$  is tensile force expected in the middle of bolt
  - $z$  is estimated lever arm



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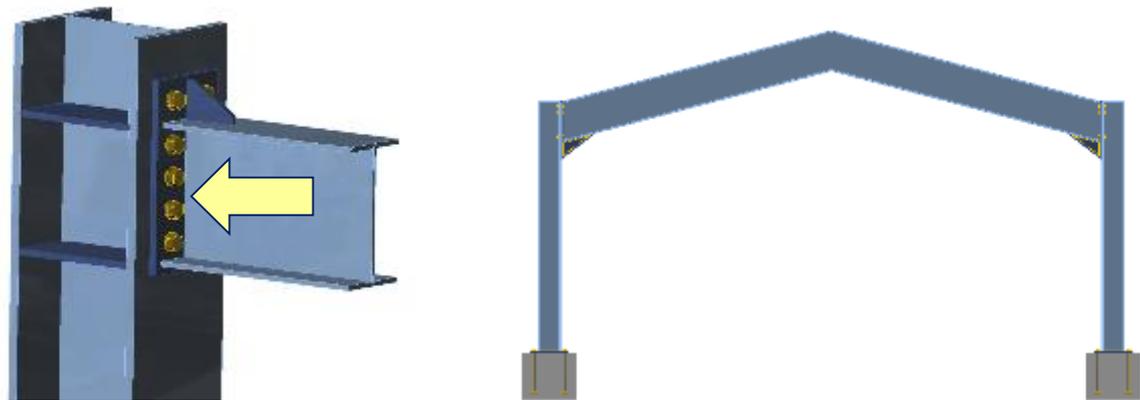
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## Summary

# Interaction of bending moment and normal force

- Many joints are exposed to interaction of bending moment and normal forces,
- One example is simple portal frame, where the bolted eaves moment connection transmits the normal force based on the rafter inclination.
  - The Normal force may be neglectable but for greater inclination is for connection significant.



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# Simplified prediction of interaction of bending moment and normal force

- In EN 1993-1-8:2005 is recommended:
  - Design moment resistance of joint  $M_{j,Rd}$  does not take account of any axial force  $N_{Ed}$  in the connected member. Axial force in the connected member  $N_{Ed}$  should not exceed 5% of design plastic resistance of connected element  $N_{pl,Rd}$ .
  - Otherwise should be considered by:
    - Linear interaction  $\longrightarrow \frac{N_{Ed}}{N_{j,Rd}} + \frac{M_{Ed}}{M_{j,Rd}} \leq 1$
    - Component method
  - Interaction ratio is calculated to the vectors between points of the interaction curve.

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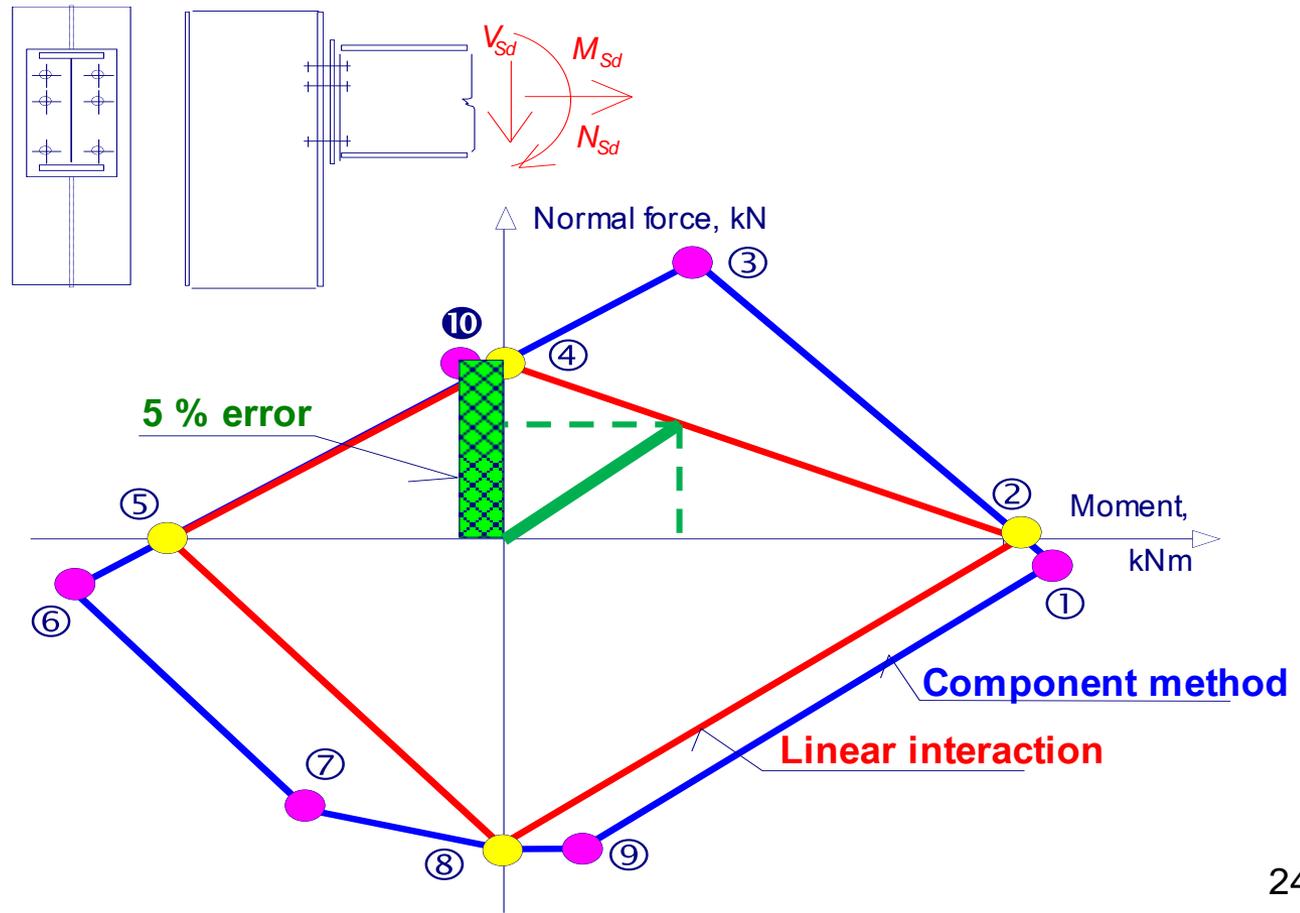
## Summary



# Interaction

## of bending moment and normal force on beam to column joint with end plate

- The significant points are marked.
- The lines represents the limit of safe design by simple linear interaction and by component method.



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## Summary

- Describe the influence to quality of design of the three major characteristics of joint
- Principles of joint classification according to What Ch. 5 in EN1993-1-8:2006
- What's influence of joint deformation due to shear force, Normal force and bending moment
- Draw the four possible representation of joints in global analyses.
- Describe the three major steps of Component method.
- How is in Component method predicted the lever arm of internal forces?
- Describe the three major steps of Component method.
- How to predict in a simple way interaction of bending moment and normal force?

# **Component Based Finite Element Method**

## **Lecture 1**

### **Beam to column moment connection**

# Material

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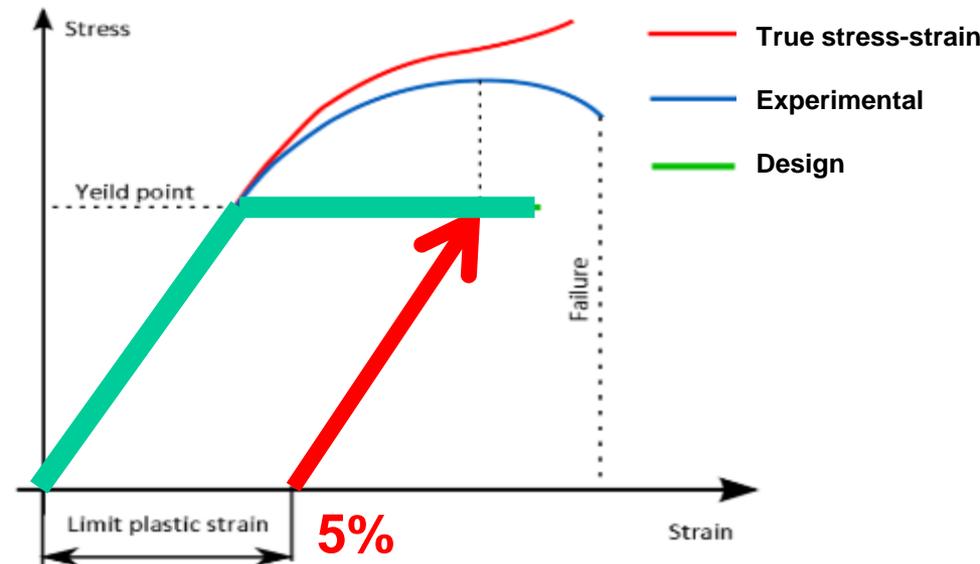
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## Summary

- Bilinear ideal elastic plastic diagram is used in design oriented models as CBFEM according to Ch. 7 in EN 1993-1-5:2006 and the slope of plastic branch is due to numerical stability  $E/1000$ .
- Plastic strain in plates is limited by 5%.
- In research oriented models is calculated the true stress-strain diagram from the material properties obtained in tensile tests, which is taken into account the necking of the coupon during its yielding before rupture.



# Plate

## Introduction

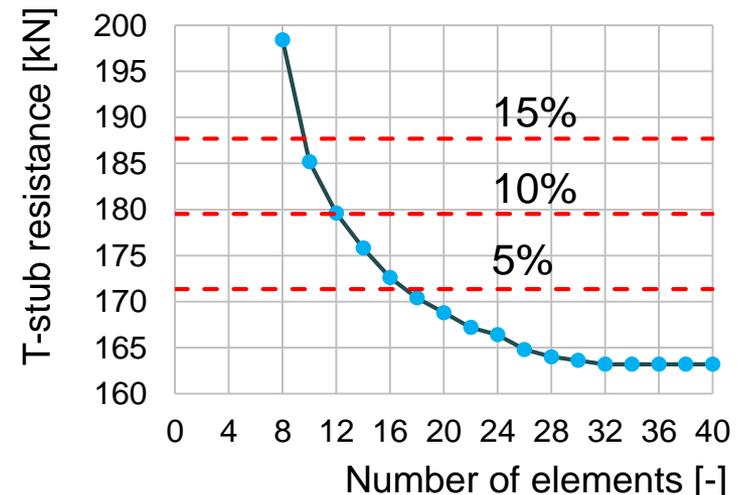
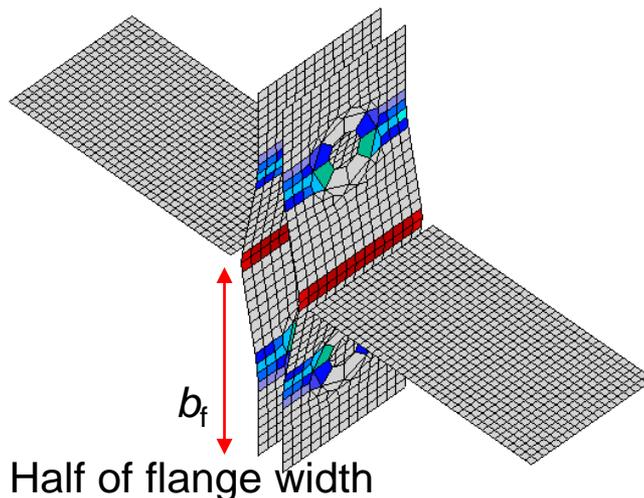
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## Summary

- Four node quadrangle shell elements are applied with six degrees of freedom, i.e. three translations and three rotations, in every node.
- End plates, element profiles, slender stiffener, T-stubs are modelled as plates connected in joint by constrains and the connection check is independent on the element size.
- Example of T-stub shows the influence of mesh size on the T-stub resistance.
  - Dashed lines are representing 5%, 10% and 15% difference.



# Bolt

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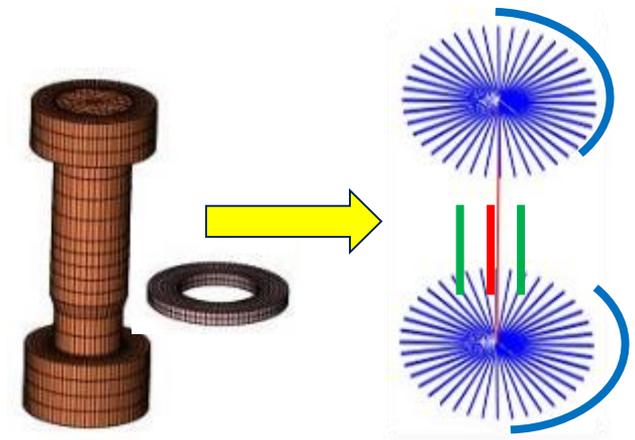
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## Summary

- Fan model with interpolation constrains to edges of bolt holes is used in CBFEM, but is used also in research oriented models (Bursi, Jaspart, 1998).
- Nonlinear springs are connected for
  - **Tension** in contact of
    - bolt shank and bolt head
  - **Shear** in contact between
    - plate and bolt head
    - bolt shank and plate



Fan model of bolt  
with **constrains**

# Working diagram of spring model for Component bolt in tension

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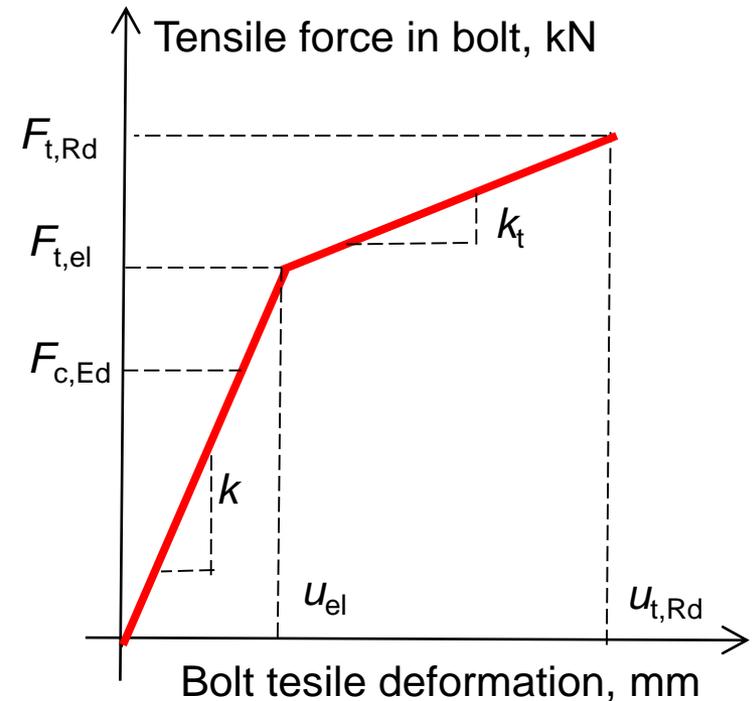
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## Summary

- For bolt's resistance is expected maximum allowed plastic strain  $\epsilon_{mpb}$  as 25 % of elongation to fracture of bolt according to EN ISO 898-1:2013, the values are summarised in Table below.
- The stiffness in tension is calculated as  $k = E A_s / L_b$ , where  $A_s$  is tensile area of bolt and  $L_b$  is the distance between the centers of the head and the bolt nut.



Maximum allowed plastic strains for bolts  $\epsilon_{t,Rd}$

Bolt grade	4.8	5.6	5.8	6.8	8.8	10.9
$\epsilon_{mpb}$ %	3,5	5,0	2,5	2,0	3,0	2,3

# Working diagram of spring model for Component bolt in shear

- Bolt in shear is simulated by bilinear diagram with its initial linear part and nonlinear one, which may be simplified as second linear one.
- Values are obtained by experiments and summarised in design standards.
- The values in Ch. 6 EN1993-1-8:2006 represents well the bearing of plate and bolt and shearing of the bolts shaft.

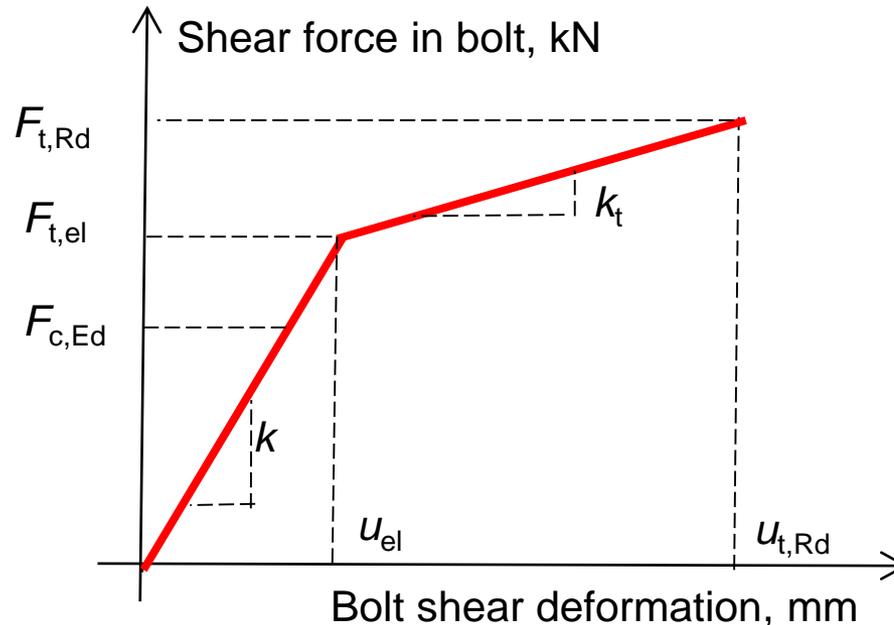
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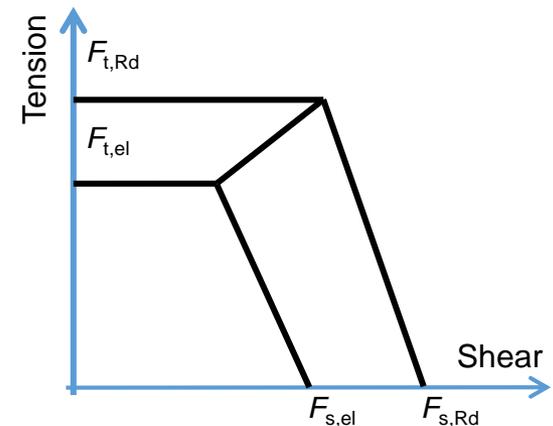
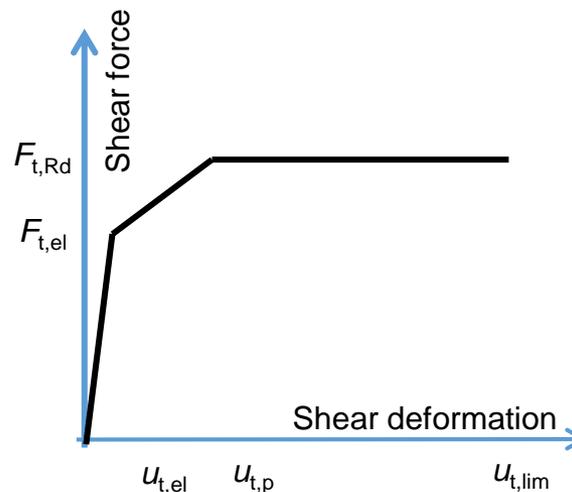
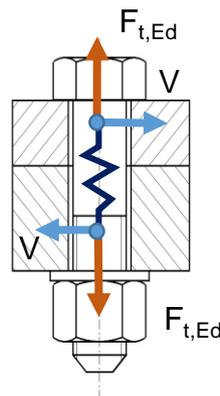
## Summary



# Bolt loaded in tension and shear

- The bolt loaded to tensile resistance  $F_{t,Rd}$  has still significant shear residual resistance  $F_{s,res,Rd}$ .
- The interaction is described by linear/nonlinear relation, which is in CBFEM simplified for initial and second part of the curve, see Figs below

$$\frac{F_{v,Ed}}{F_{v,Rd}} + \frac{F_{t,Ed}}{1,4 F_{t,Rd}} \leq 1,0$$



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# Bolts

- Interaction diagram for deformation of the bolt loaded in shear and tension, (Wald et al. 2016)

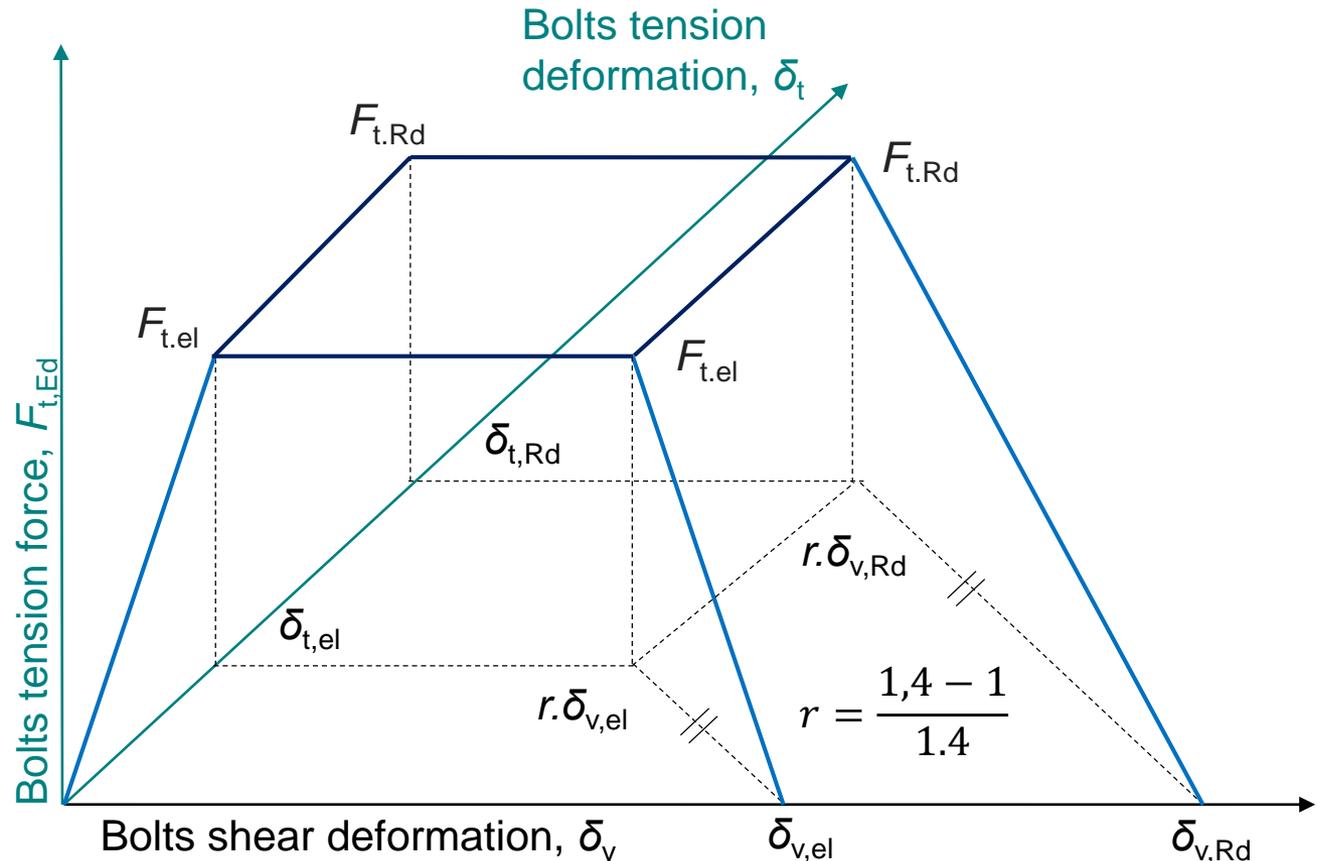
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# Slip resistant bolt

- In the preloaded slip resistant bolt is transferred the shear force by friction.
- As the friction force is reached slip resistance the shear force is transferred by bearing of the plate and shearing of bolt as regular non preloaded bolt.
- Bolt is preloaded to 70% of its strength.

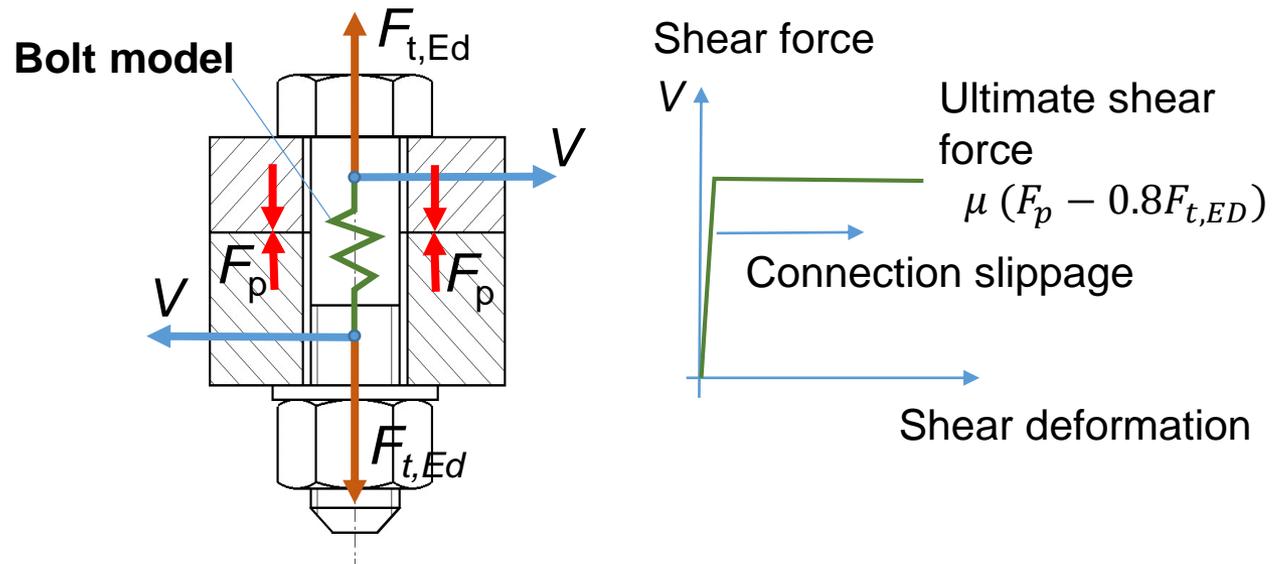
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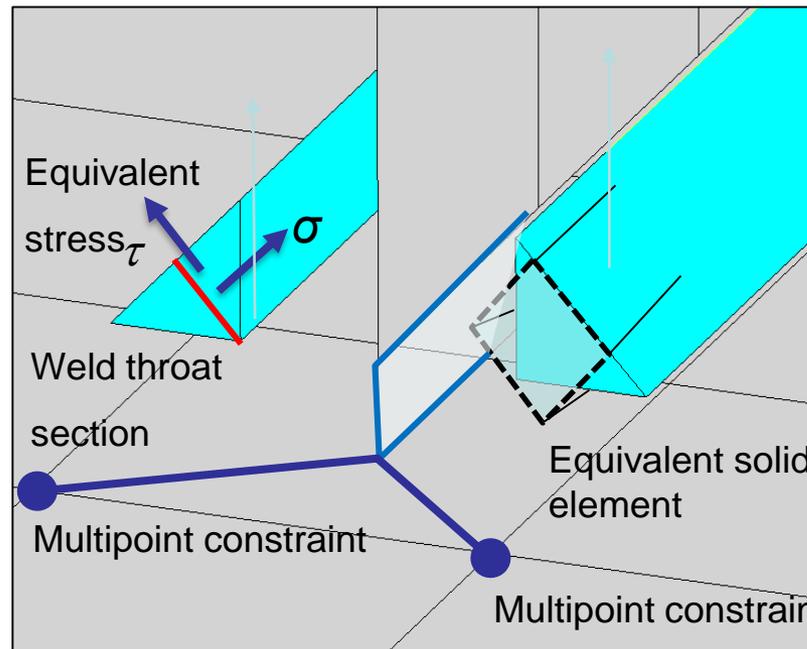
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# Welds

- Filled weld is modelled by equivalent solid elastoplastic element, which is added between plates to express the weld behaviour, see Fig. below.
- The element respects the weld throat thickness, position, and orientation to assure good representation of weld deformation stiffness, resistance and deformation capacity.
- The plastic strain in weld is limited to 5%.



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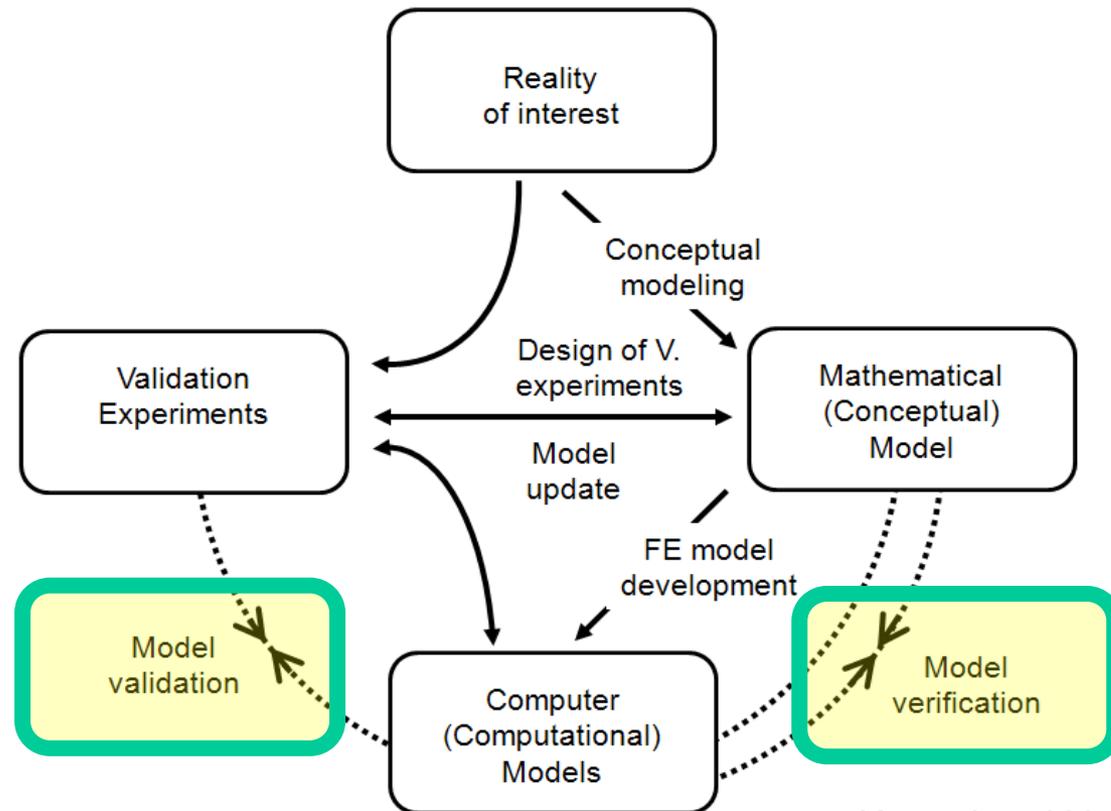
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# Verification & Validation

- The need and position of Verification & Validation in prediction of the reality is demonstrated on the diagram below.



Kwasniewski L. (2009)

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- **Validation**
  - compares the numerical solution with the experimental data.
- **Verification**
  - uses comparison of computational solutions with highly accurate analytical or numerical solution.
- **Benchmark case**
  - is an example for check of the software and its user by validated and simplified input and output.

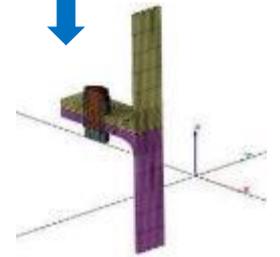
# Design and research oriented model

Current approval of design models consist of

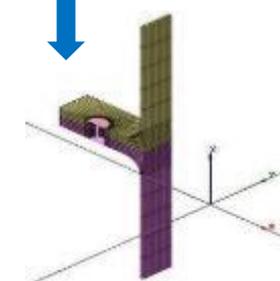
- 1) **Experiments**
- **Research oriented FE model** (ROFEM)
  - 2) is **validated** on experiment.
  - 3) Numerical experiments are prepared.
- **Design oriented analytical/numerical model** (AM/DOFEM)
  - 4) is **verified** to numerical experiments and/or another design models.
  - 5) Sensitivity study is prepared.
  - 6) Validity range is defined.
- **Benchmark case** (BC)
  - 7) is prepared to help the users of model to check up its correctness and proper use.



Experiment



Research model



Design model

## Introduction

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General

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Verification

Benchmark case

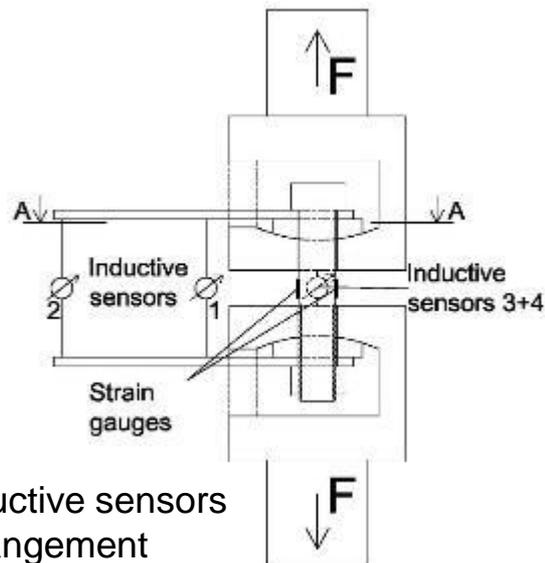
Assessment II

## Summary

# Experiments with bolts in tension

- Out of dozens of published tests, 13 bolts of different lengths and diameter were tested to obtain the detailed force-deformation behaviour.
- Bolts elongation was measured by inductive sensors.
- Bolts were fixed to the testing machine by special tools with bearing caps to ensure hinges on its ends.

Testing machine



Inductive sensors arrangement



## Introduction

Design models  
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Component meth.  
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Assessment I

## CBFEM

General

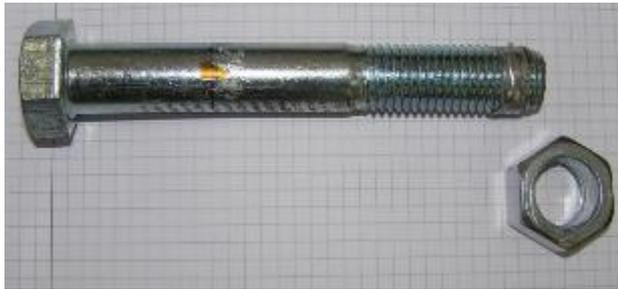
## Validation

Verification  
Benchmark case  
Assessment II

## Summary

# Failure modes of bolts in tension

- There are four possible failure modes of bolts loaded in tension:



Stripping of nut threads



Rupture of bolt close to nut



Stripping of bolt threads



Rupture of bolt close to head

## Introduction

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Assessment I

## CBFEM

General

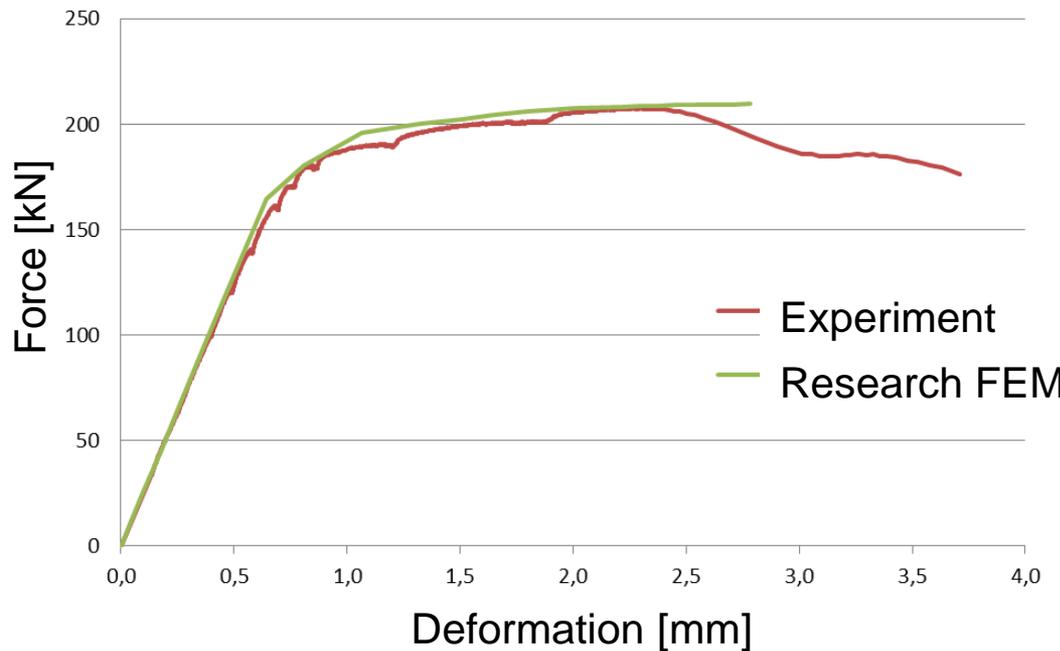
## > Validation

Verification  
Benchmark case  
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## Summary

# Validation for rupture of bolt close to head

- The figure shows the validation of research oriented model in case of failure mode rupture of bolt close to the bolt head.



Research oriented model of bolt



Rupture of bolt close to head

## Introduction

- Design models
- Global analyse
- Classification
- Component meth.
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## CBFEM

- General

## Validation

- Verification

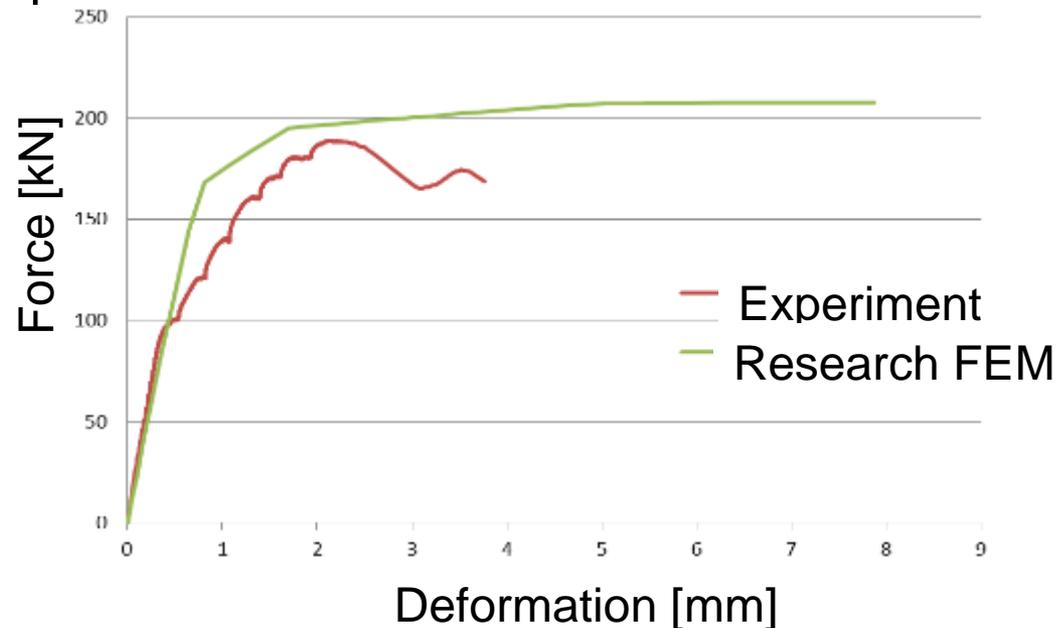
- Benchmark case

- Assessment II

## Summary

# Validation of stripping of nut thread

- The validation of the research oriented model in case of failure mode stripping of the nut thread is presented below.



Research oriented model of bolt



Stripping of nut threads

## Introduction

- Design models
- Global analyse
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- Interaction
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## Validation

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## Summary

# Experiment with T-stub in tension

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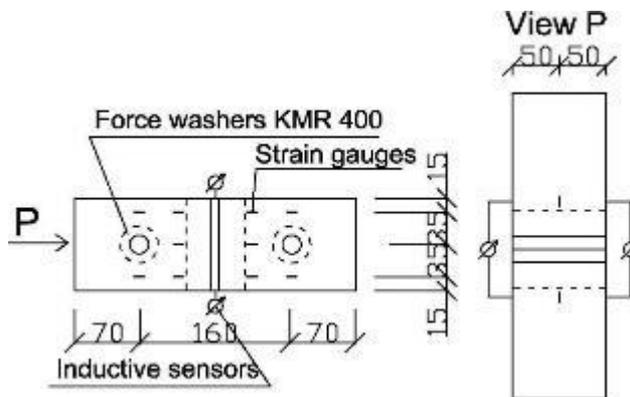
General

## Validation

Verification  
Benchmark case  
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## Summary

- Two specimens were prepared with T stubs, cross sections HEB300 and HEB400 with bolts M24 8.8.
- T-stub deformation was measured by inductive sensors.
- Strains were measured on the expected yielding lines on flanges by strain gauges.
- Forces in the bolts were measured by KMR400 rings placed under the bolt heads.



Measuring devices arrangement



Testing machine

# Validation of research model of T-stub in tension

- The Figure shows the validation of the research oriented model of T-stub from HEB300 loaded in tension.

## Introduction

Design models  
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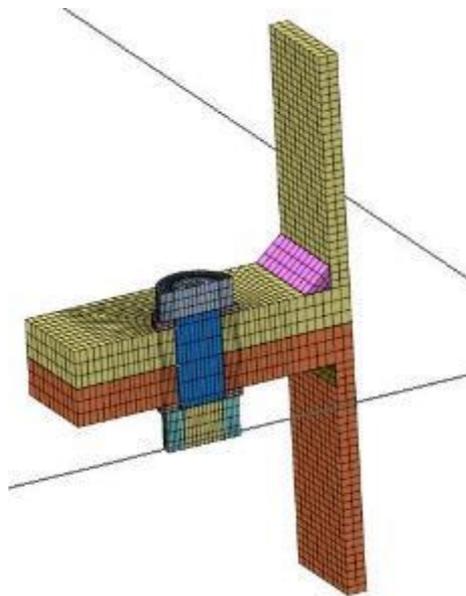
## CBFEM

General

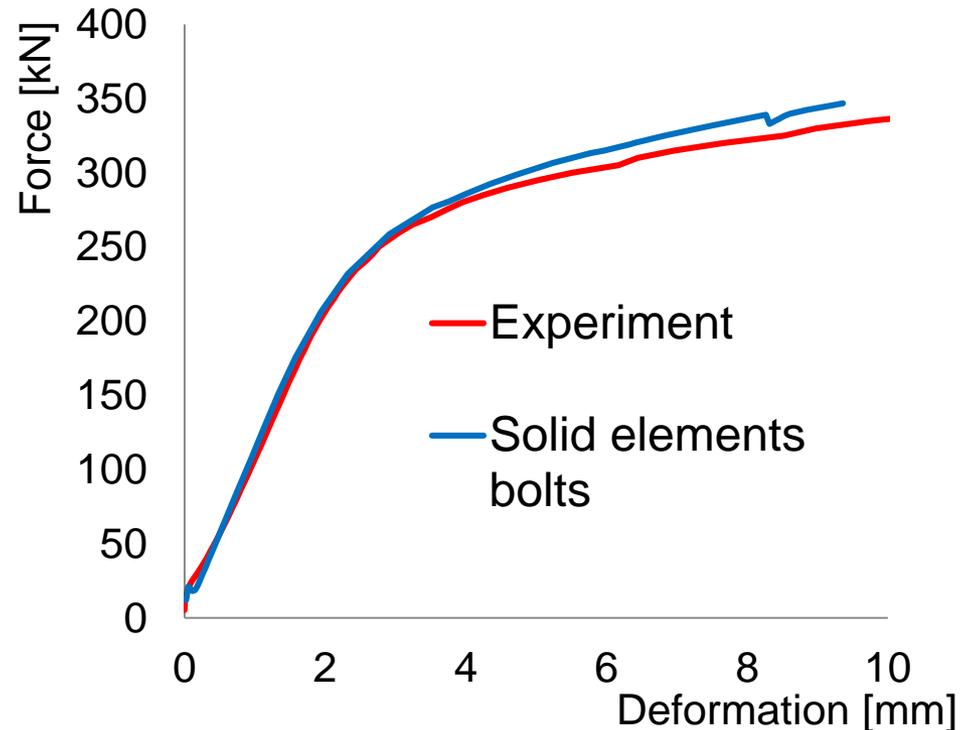
## Validation

Verification  
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## Summary



Research oriented model of T-stub



# Experiments with generally positioned end plates

- The experiments were prepared with three bolted beam to beam end plate connections.

## Introduction

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Assessment I

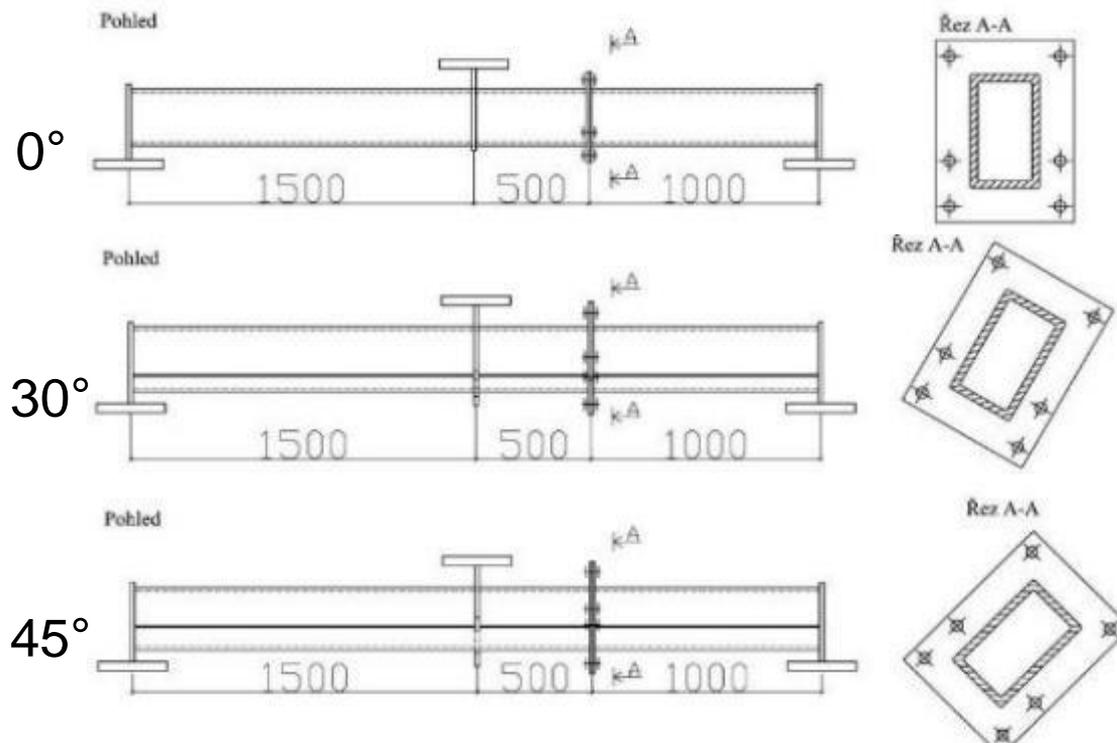
## CBFEM

General

## Validation

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## Summary



# Parameters of specimens for the generally positioned end plate

- Plate **P20** – 400 x 300 mm
- Steel **S355** ( $f_{y,exp} = 410$  MPa;  $f_{u,exp} = 582$  MPa)
- Bolts **M20** - 8.8
- Pitches           vertical (35 – 230 – 100 - 35 mm)  
                          horizontal (30 – 240 – 30 mm)

## Introduction

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General

## Validation

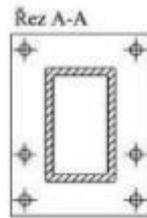
Verification

Benchmark case

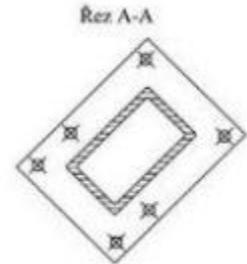
Assessment II

## Summary

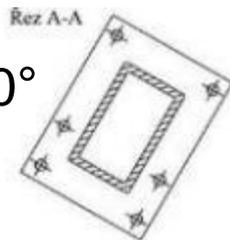
0°



45°

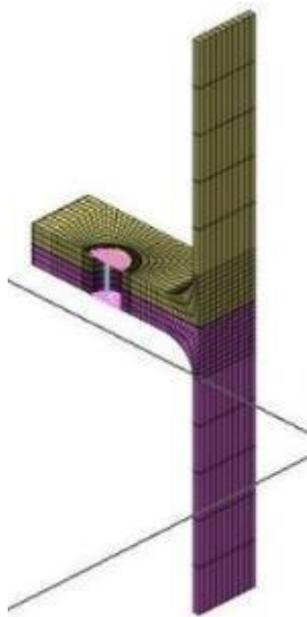


30°

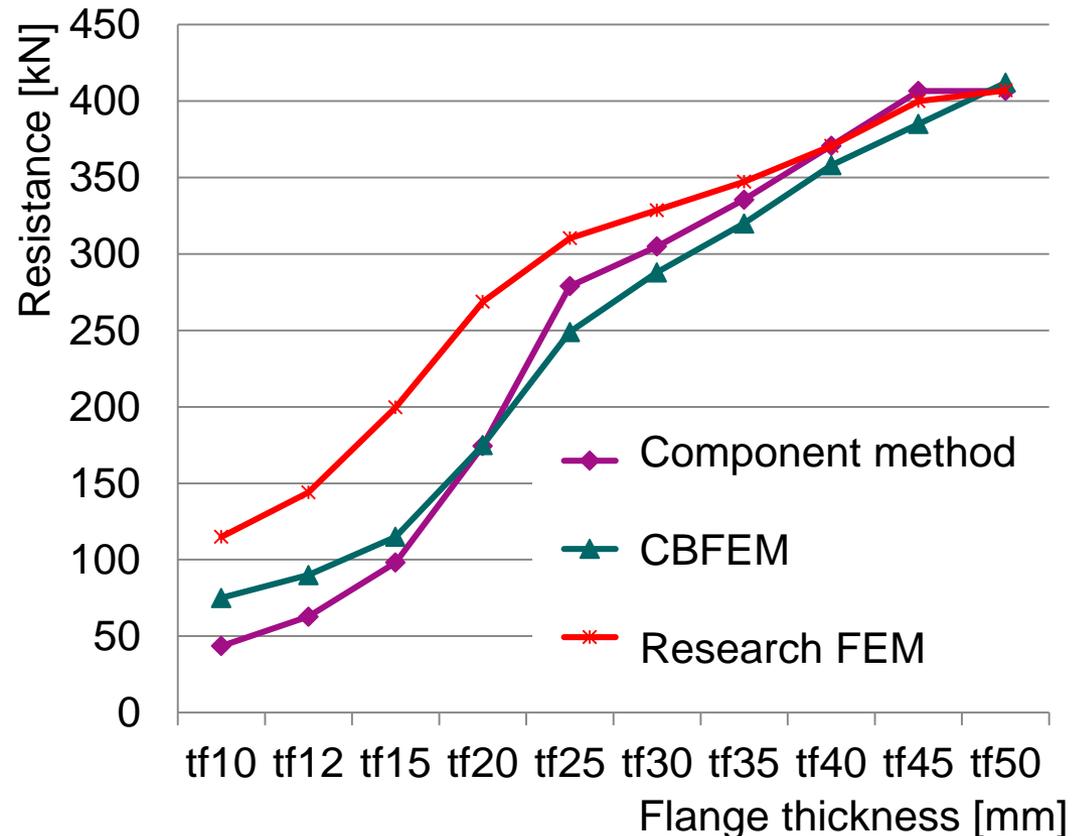


# Verification of T-stub in tension

- The Figure shows the verification of the design oriented model of T-stub from HEB300 loaded in tension to research oriented FE model. Comparison to component method is included.



Design oriented model of T-stub



## Introduction

- Design models
- Global analyse
- Classification
- Component meth.
- Interaction
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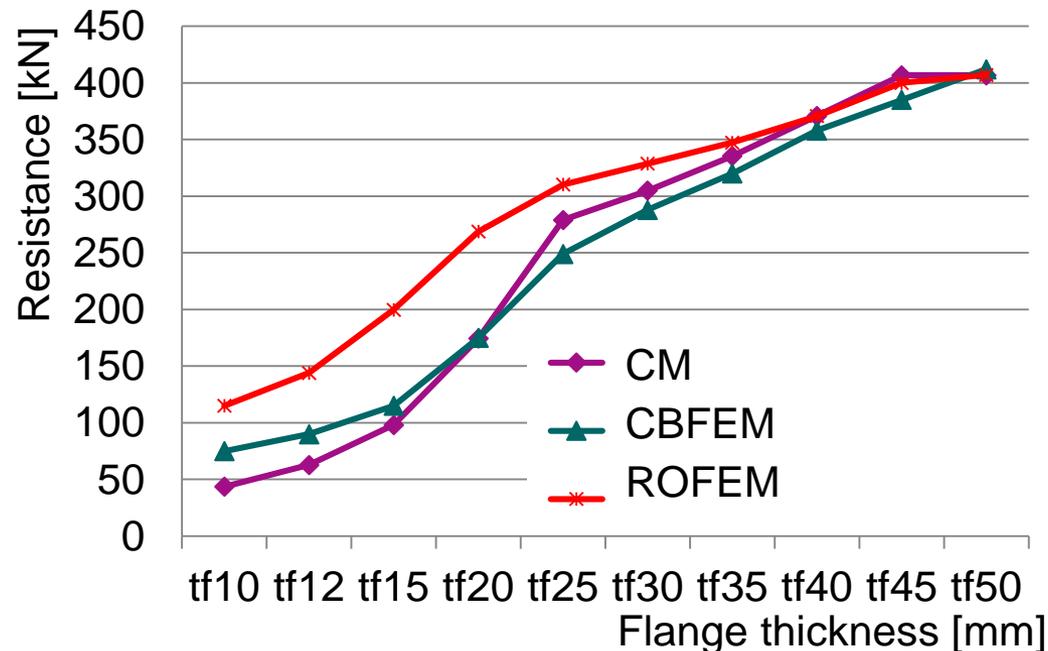
## CBFEM

- General
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## Summary

# Verification of T-stub in tension

- The sensitivity study of thickness of the flange shows higher resistance according to CBFEM compared to CM for samples with flange thicknesses up to 20 mm.
- ROFEM gives even higher resistance for these samples.
- Higher resistance of both numerical models is due to neglect of membrane effect in CM.



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## CBFEM

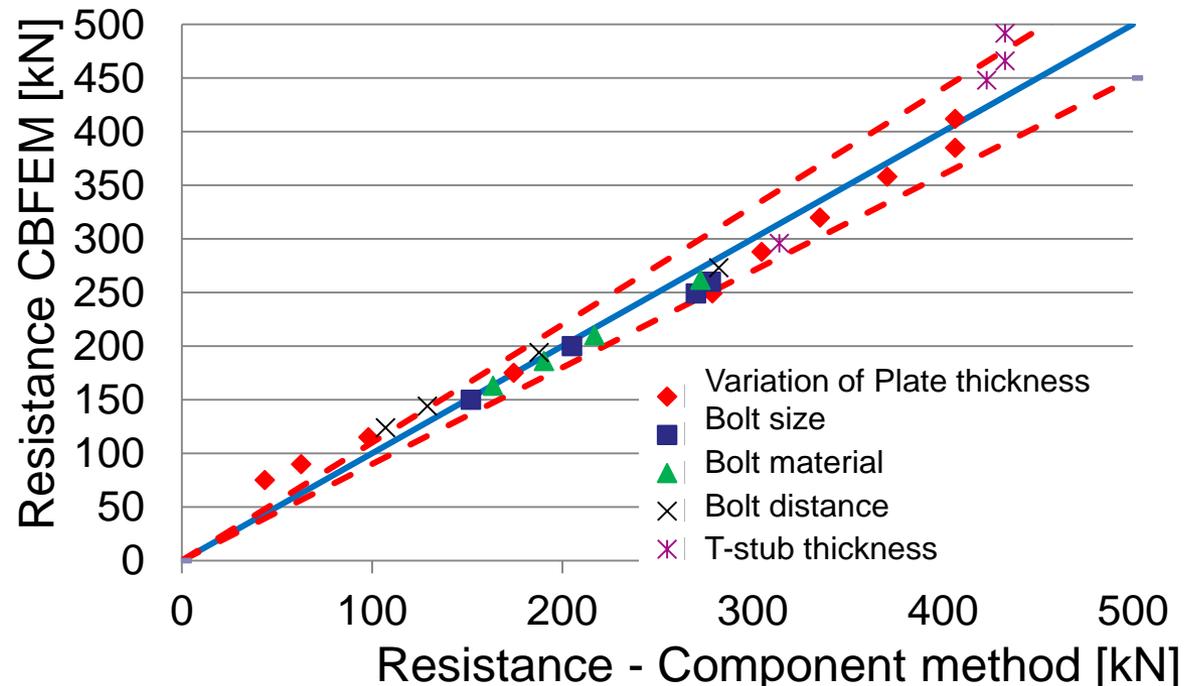
General  
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## Summary



# Verification of T-stub in tension

- To show the prediction of the CBFEM model, results of the studies are summarized in graph comparing resistances by CBFEM and component method. The results show that the difference of the two calculation methods is mostly up to 10%.
- In cases with  $CBFEM/CM > 1,1$  accuracy of CBFEM is verified by the results of Research oriented FEM, which gives highest resistance in all selected cases.



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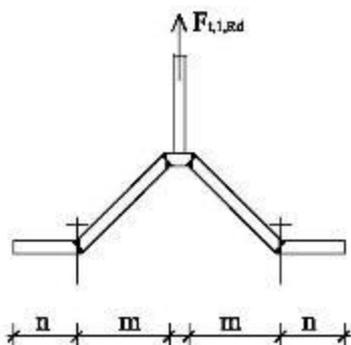


# Verification of T-stub in tension

- Three failure modes of T-stub are considered.

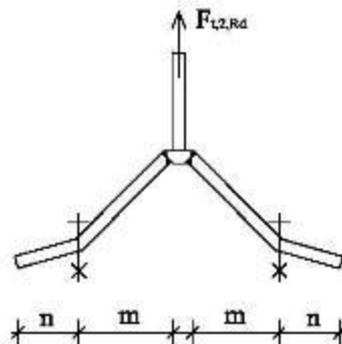
## Component Method

Full yielding of flange



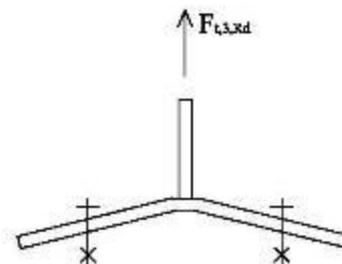
$$F_{t,1,Rd} = \frac{(8n - 2e_w) M_{pl,1,Rd}}{2mn - e_w(m+n)}$$

Yielding of flange and rupture of bolts



$$F_{t,2,Rd} = \frac{2M_{pl,2,Rd} + 2nF_{t,Rd}}{m+n}$$

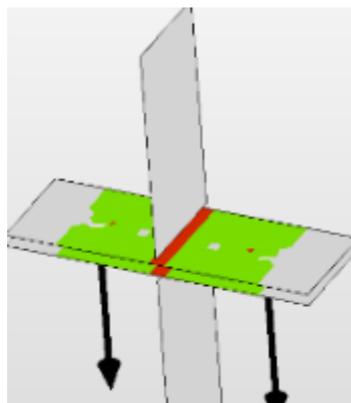
Rupture of bolts



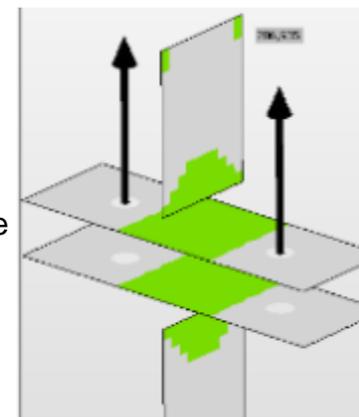
$$F_{t,3,Rd} = 2F_{t,Rd}$$

## Component Based FEM

Yielding of flange



Bolt resistance



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### Summary

# Verification of generally loaded end plate

- Resistance calculated by CBFEM is compared with the results of CM and experimental results. The sensitivity study is focused on ratio of bending moments in strong and weak axis, see Figure below.
- CM with linear interaction gives conservative values of resistance.
- CM with quadratic interaction gives the highest resistances, which are to experimental results still rather conservative.
- CBFEM gives similar results as CM with quadratic interaction.

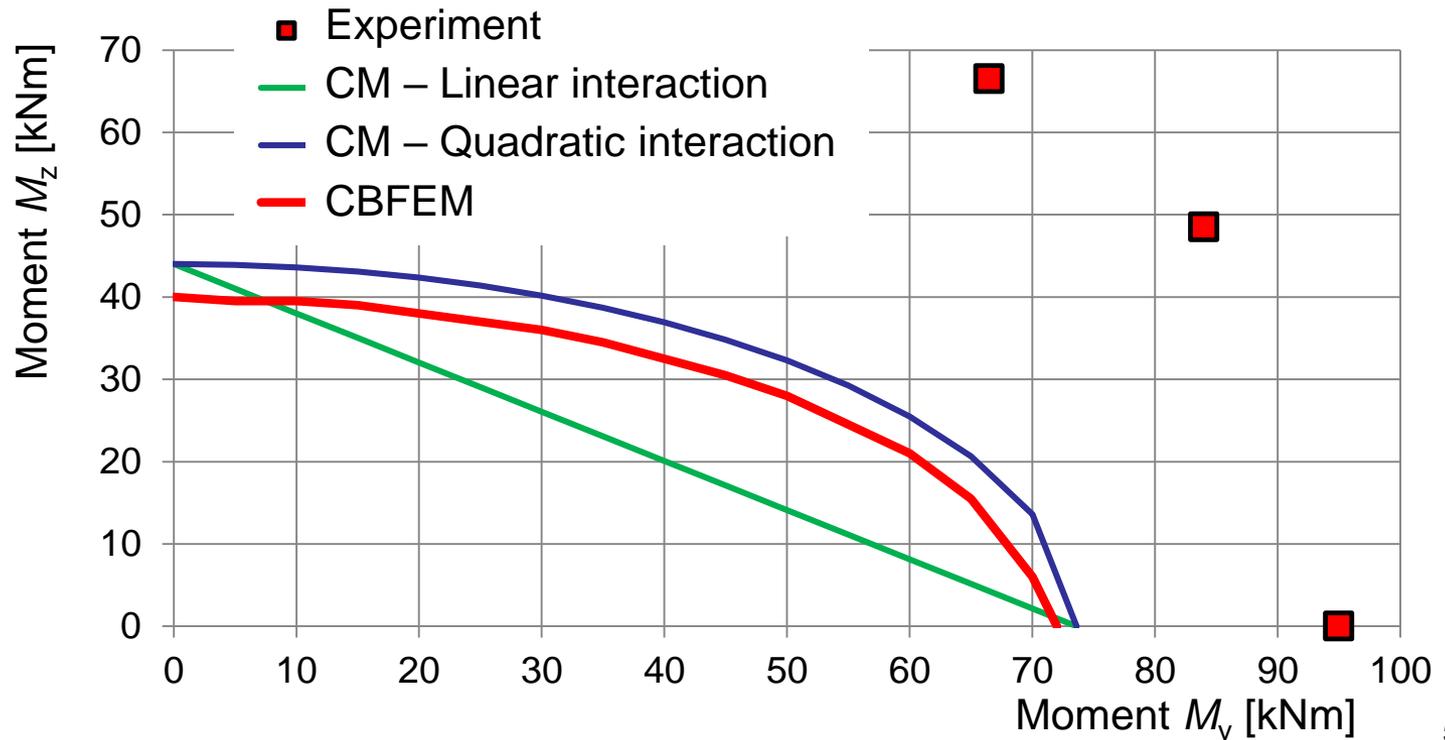
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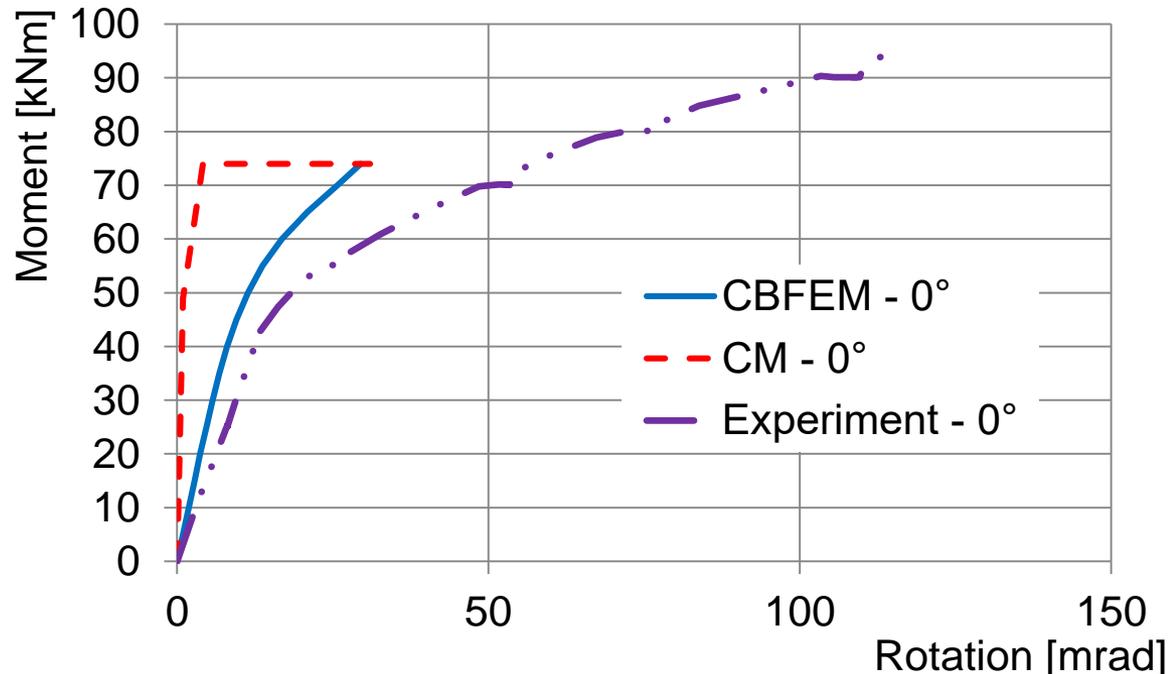
General  
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## Summary



# Verification of end plate

- Comparison of the global behaviour described by moment-rotation diagram is prepared. Attention is focused to initial stiffness, resistance and deformation capacity.
- Sample  $0^\circ$  with strong axis bending moment is chosen to present as reference, see Figure below.
- CM gives higher initial stiffness compared to CBFEM and experimental data.
- Resistance predicted by CM and CBFEM are similar.
- Experimentally reached resistance is higher.



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# Benchmark case T-stub

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## Summary

### ○ Inputs

### ○ T-stub

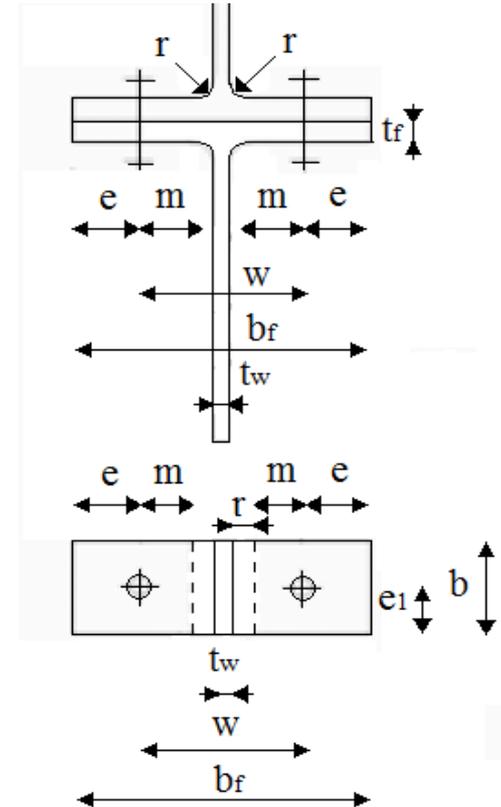
- Steel S235
- Flange thickness  $t_f = 20$  mm
- Web thickness  $t_w = 20$  mm
- Flange width  $b_f = 300$  mm
- Length  $b = 100$  mm
- Double fillet weld  $a_w = 10$  mm

### ○ Bolts

- 2 x M24 8.8
- Distance of the bolts  $w = 165$  mm

### ○ Outputs

- Design resistance in tension  $F_{T,Rd} = 175$  kN
- Collapse mode - full yielding of the flange with maximal strain 5 %
- Utilization of the bolts 88,4 %
- Utilization of the welds 49,1 %



# Benchmark case end plate connection

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➤ Benchmark case  
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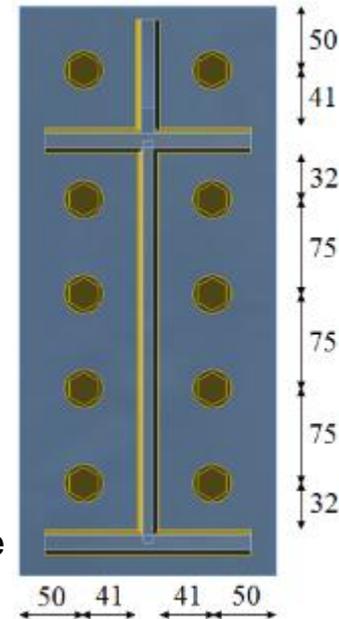
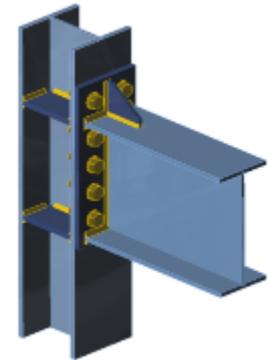
## Summary

### Inputs

- Steel S235
- Beam IPE 330
- Column HEB 300
- End plate height  $h_p = 450$  (50-103-75-75-75-73) mm
- End plate width  $b_p = 200$  (50-100-50) mm
- End plate P15
- Column stiffeners 15 mm thick and 300 mm wide
- End plate stiffener 10 mm thick and 90 mm wide
- Flange weld throat thickness  $a_f = 8$  mm
- Web weld throat thickness  $a_w = 5$  mm
- Bolts M24 8.8

### Outputs

- Design resistance in bending  $M_{Rd} = 209$  kNm
- Corresponding vertical shear force  $V_{Ed} = 209$  kN
- Collapse mode - yielding of the beam stiffener on upper flange
- Utilization of the bolts 89,5 %
- Utilization of the welds 87,2 %



# Assessment II

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› Assessment II

**Summary**

- How is limited plastic strain for design of resistances of plates?
- How is simplified the convergence of finite elements procedure of steel members and plates?
- How is modelled the bolt model in CBFEM?
- How is modelled interaction bolts loaded at the same time in shear and tension?
- As how is transferred the shear force as the slip resistance bolt reach its resistance?
- Why is filled weld modelled by equivalent solid elastoplastic element, which is added between plates?
- How differs validation from verification?
- What are two major purposes of benchmark cases in application of FEA analyses?

# Summary

## Lecture 1

### Beam to column moment connection

# Summary

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## ▶ Summary

- The design of beam to column moment connections is focussed to preferable yielding of steel plates and brittle failure of fasteners, bolts, welds.
- The design of beam to column moment connection by Component Method (CM) is very accurate in components behaviour modelling.
- The lever arm is in CM estimated based on the best engineering practice. Its prediction is good in well know and tested connections and joints. Its educated guess affects the resistance.
- The CM is prepared for software tools and design tables not for had calculation.



# Summary

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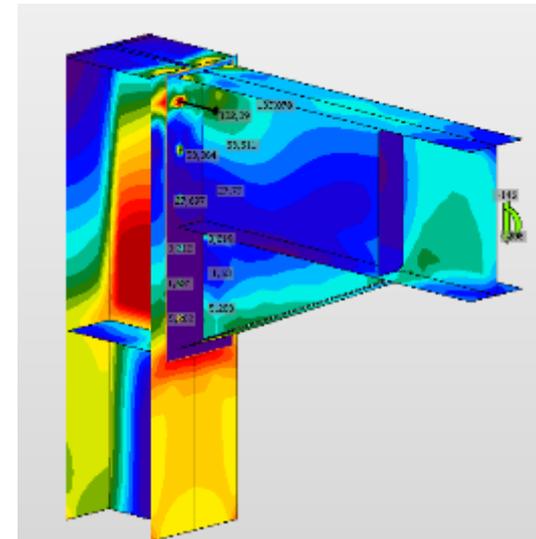
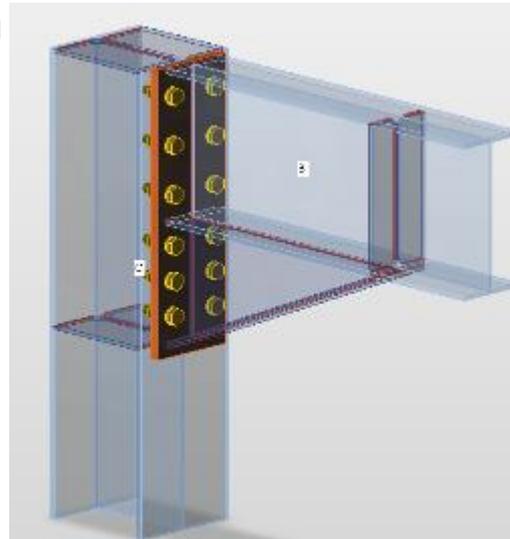
- The design of connections by finite element method is not replication of the physical experiment. The designer is interested into the limited yielding of steel plates and failure of fasteners.
- Component based finite element method (CBFEM) is taking advantage of accurate modelling of component behaviour based on experiment and accuracy of discrete analyse of steel plate by FEM
- The Validation and Verification procedure is integral part of any finite element analyses. The procedure is checking the software and the use by designer.
- CBFEM offers the designer a discrete view on the behaviour, see next slides.



# Prediction of global and local behaviour

## Beam to column connection

- Full depth end plate 25 mm
- Rafter IPE 400
- Column HEA 320
- 12 bolts M24 8.8
- Haunch 700x300 mm
- Flange 15x150 mm
- Stiffeners P20
- Steel S355



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### Summary

# Global and local behaviour

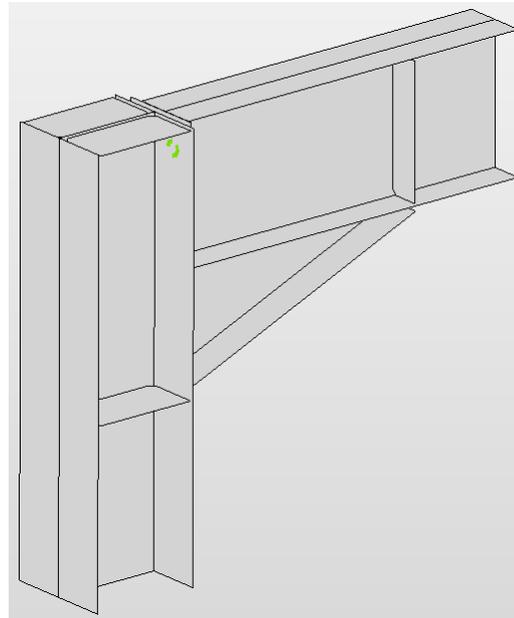
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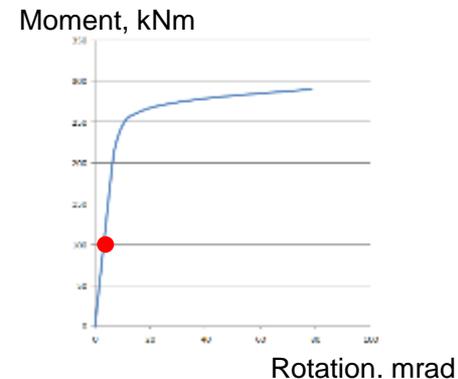
## Summary



$$M = 100 \text{ kNm}$$

$$F_i = 3,2 \text{ mrad}$$

$$S_i = 31,6 \text{ MNm/rad}$$



## Column flange plastification round bolts

Well designed steel connection starts to classify early to allow plastic distribution of forces between connectors.

# Global and local behaviour

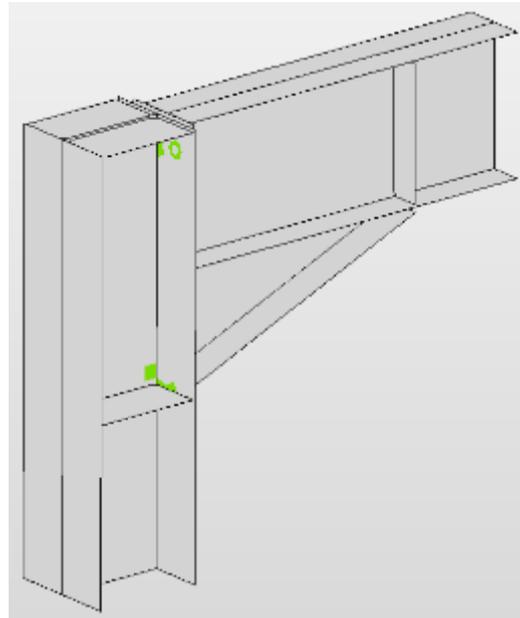
## Introduction

- Design models
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## CBFEM

- General
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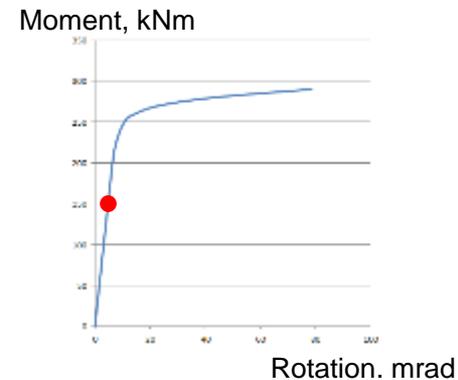
## Summary



$$M = 150 \text{ kNm}$$

$$F_i = 4,8 \text{ mrad}$$

$$S_i = 31,6 \text{ MNm/rad}$$



## Column web plastification

# Global and local behaviour

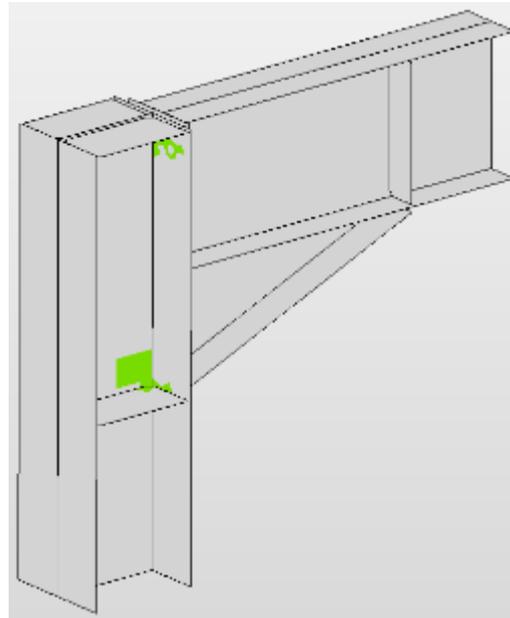
## Introduction

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- General
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## Summary

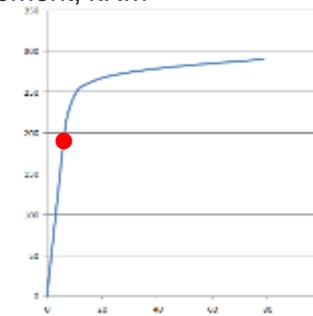


$$M = 180 \text{ kNm}$$

$$F_i = 5,7 \text{ mrad}$$

$$S_i = 31,5$$

Moment, kNm



Rotation. mrad

## Progress of column web plastification

# Global and local behaviour

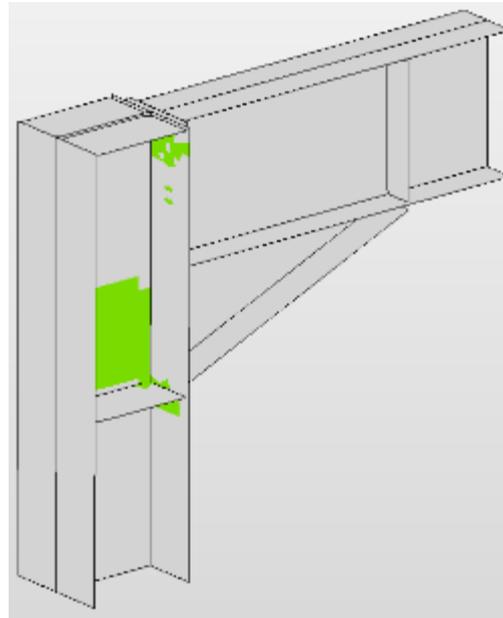
## Introduction

- Design models
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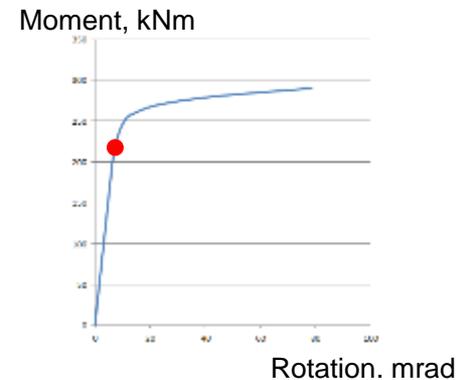
## Summary



$M = 220 \text{ kNm}$

$F_i = 7,3 \text{ mrad}$

$S_i = 30,0 \text{ MNm/rad}$



## Progress of column web plastification

# Global and local behaviour

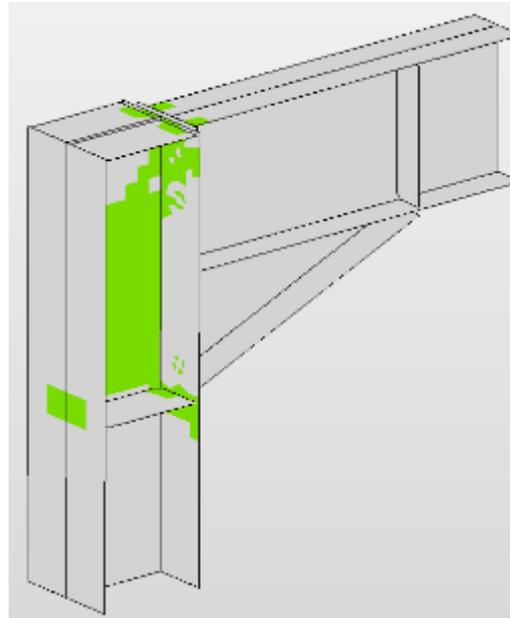
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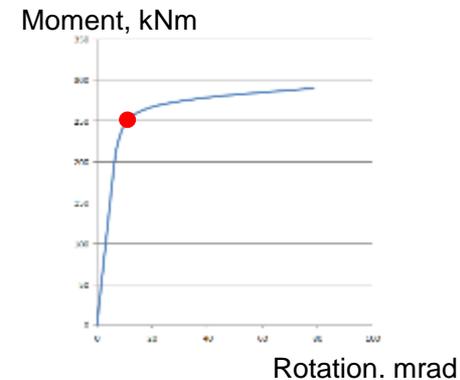
## Summary



$$M = 250 \text{ kNm}$$

$$F_i = 10,7 \text{ mrad}$$

$$S_i = 23,4 \text{ MNm/rad}$$



Column web full plastification

# Global and local behaviour

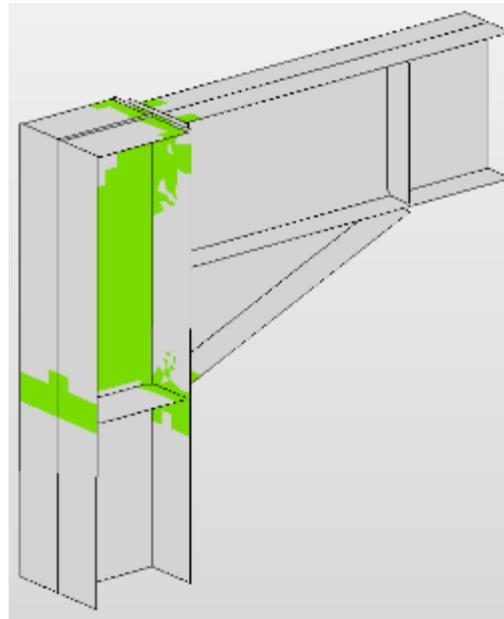
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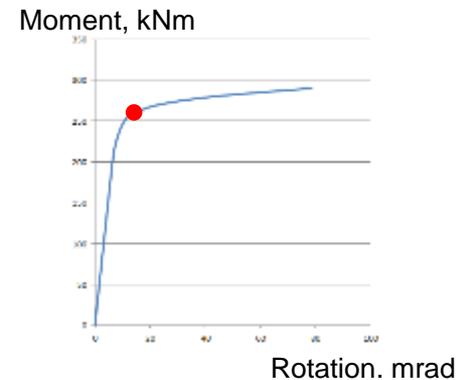
## Summary



$M = 260 \text{ kNm}$

$F_i = 14,7 \text{ mrad}$

$S_i = 17,4 \text{ MNm/rad}$



Column flange on opposite side plastification

# Global and local behaviour

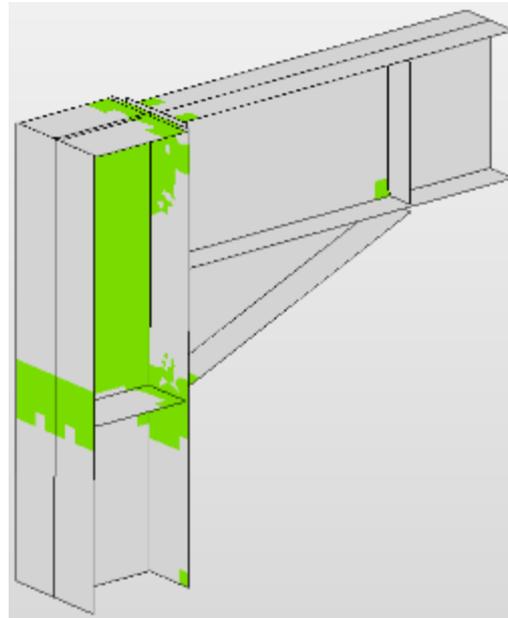
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- Benchmark case
- Assessment II

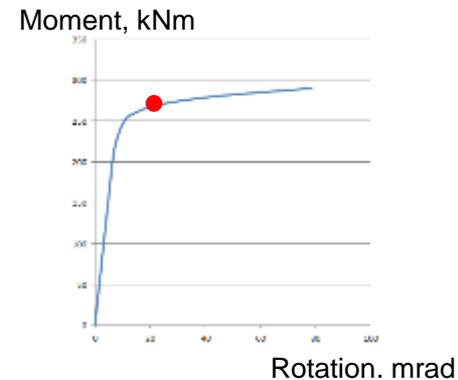
## Summary



$$M = 270 \text{ kNm}$$

$$F_i = 23,4 \text{ mrad}$$

$$S_i = 11,5 \text{ MNm/rad}$$



Beam above haunch starts yield

# Global and local behaviour

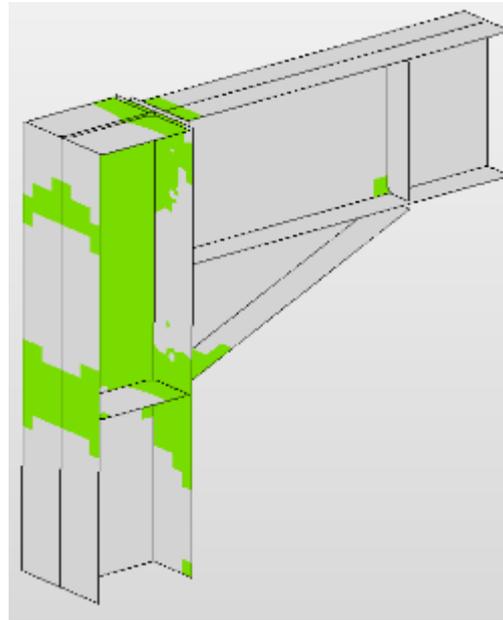
## Introduction

- Design models
- Global analyse
- Classification
- Component meth.
- Interaction
- Assessment I

## CBFEM

- General
- Validation
- Verification
- Benchmark case
- Assessment II

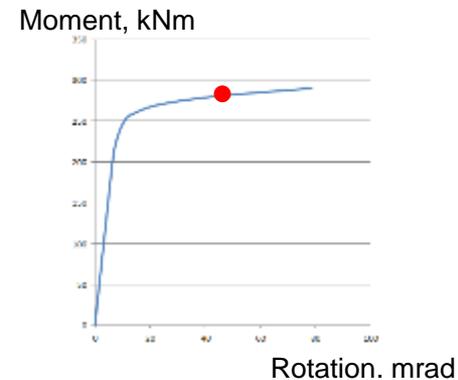
## Summary



$$M = 280 \text{ kNm}$$

$$F_i = 43,6 \text{ mrad}$$

$$S_i = 6,4 \text{ MNm/rad}$$



Further plastification

# Global and local behaviour

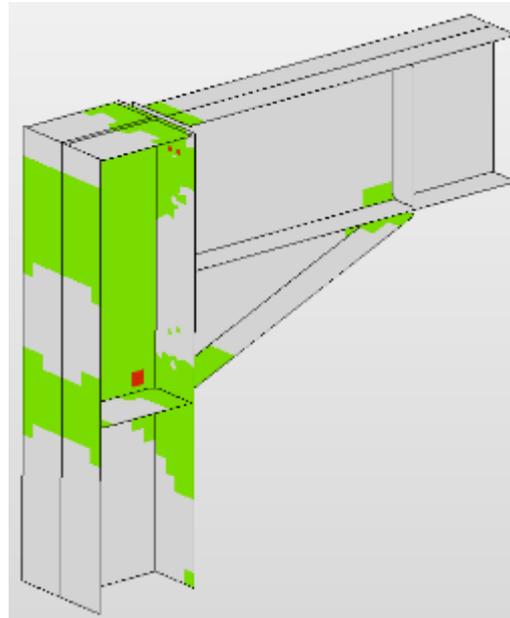
## Introduction

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Classification  
Component meth.  
Interaction  
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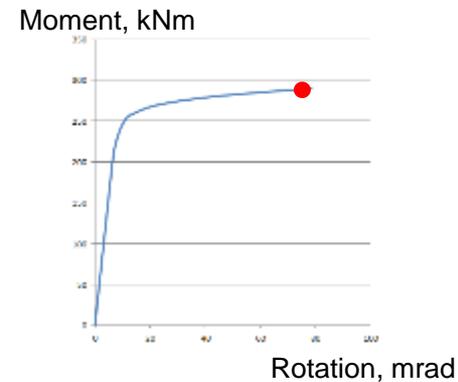
## Summary



$M = 290 \text{ kNm}$

$F_i = 78,6 \text{ mrad}$

$S_i = 3,7 \text{ MNm/rad}$



## Resistance reached

- By 5% strain in column web loaded in shear and compression.
- **Well designed steel connection** starts to plasticize early to allow plastic distribution of forces between connectors/plates.

# Global and local behaviour

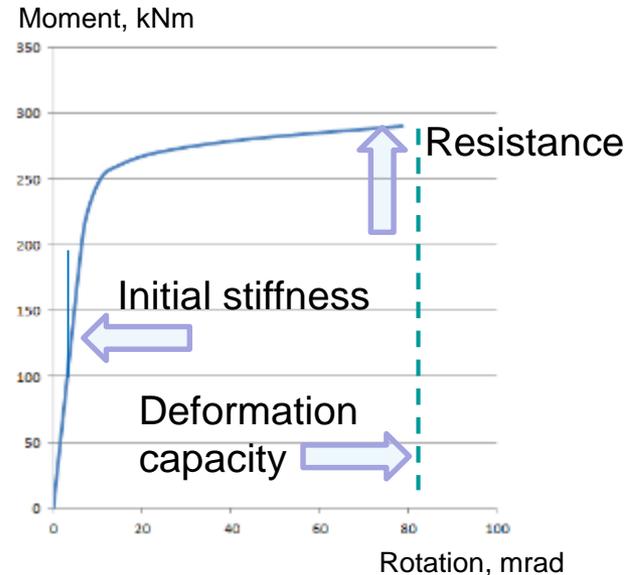
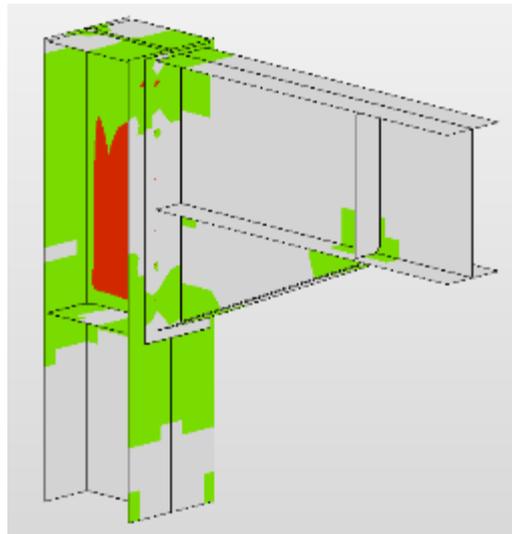
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## Summary



## The major joint in bending design characteristics

where  $S_{j,ini}$  is the initial stiffness,  
 $M_{j,Rd}$  is the design bending resistance,  
 $\varphi_{Cd}$  is the deformation capacity  
are well described.

# What is the major reason

of using CBFEM for Beam to column moment connections ?

## Introduction

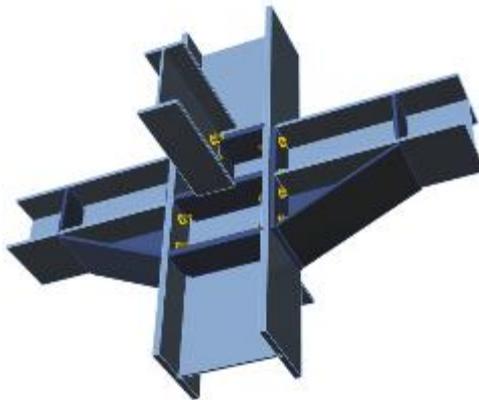
Design models  
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## CBFEM

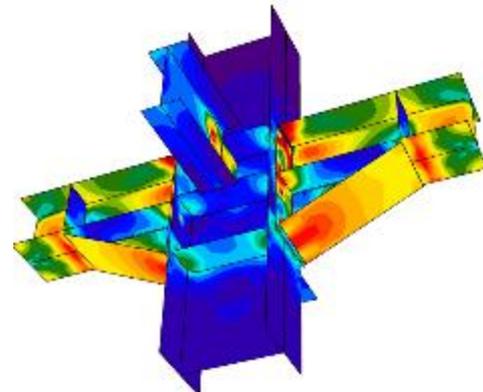
General  
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## Summary

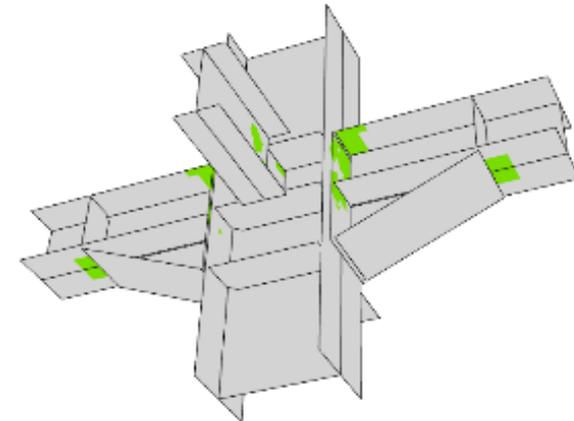
- **Generally loaded complex joints** is difficult to design in space accurately by Component or other methods.
- The example of design procedure by CBFEM is shown below.



3D model



Finite element analyses



Design check



# Thank your for attention

**URL: [steel.fsv.cvut.cz](http://steel.fsv.cvut.cz)**

**František Wald, Lukáš Gödrich, Marta Kuříková  
Luboš Šabatka, Jaromír Kabeláč, Drahoš Kojala**

# Notes to users of the lecture

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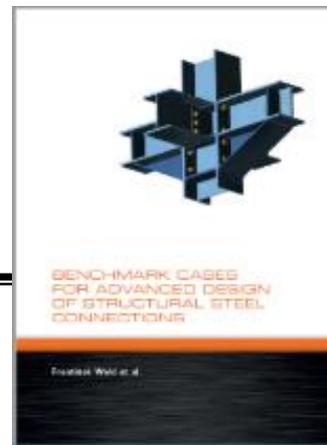
- Subject Design of the open sections joints.
- Lecture duration 60 mins.
- Keywords Civil Engineering, Structural design, Steel structure, Beam to column connection, Beam to beam connection, Beam splices, Open section, Joint, Component Method, Component based Finite Element Method, Eurocode.
- Aspects to be discussed Experiments, Reasons and methods of classification, Principles of CM, Major components in CM, Interaction of forces, Components in CBFEM, Principles of CBFEM, Validation and Verification.
- Further reading relevant documents in references and relevant European design standards, Eurocodes including National Annexes.
- Preparation for tutorial exercise see examples in References.

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# Standards

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- EN1993-1-5, Eurocode 3, Design of steel structures, Part 1-5, Plated Structural Elements, CEN, Brussels, 2005.
- EN1993-1-8:2006, Eurocode 3, Design of steel structures, Part 1-8, *Design of joints*, CEN, Brussels, 2006.
- EN1994-1-1:2010, Eurocode 4, Design of composite steel and concrete structures, Part 1-1, *General rules and rules for buildings*, CEN, 2010.
- ISO 898-1, Mechanical properties of fasteners made of carbon steel and alloy steel, Part 1, Bolts, screws and studs with specified, property classes, Coarse thread and fine pitch thread, Geneva, 2013